

**JEE MAINS-2011****IMPORTANT INSTRUCTIONS**

1. Immediately fill in the particulars on this page of the Test Booklet with Blue/Black Ball Point Pen. Use of pencil is strictly prohibited.
2. The Answer Sheet is kept inside this Test Booklet. When you are directed to open the Test Booklet, take out the Answer Sheet and fill in the particulars carefully.
3. The test is of 3 hours duration.
4. The Test Booklet consists of 90 questions. The maximum marks are 360.
5. There are three parts in the question paper A, B, C consisting of Chemistry, Physics and Mathematics having 30 questions in each part of equal weightage. Each question is allotted 4 (four) marks for each correct response.
6. Candidates will be awarded marks as stated above in instruction No.5 for correct response of each question. 1/4 (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
7. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 6 above.
8. Use Blue/Black Ball Point Pen only for writing particulars/markings responses on Side-1 and Side-2 of the Answer Sheet. Use of pencil is strictly prohibited.
9. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc., except the Admit Card inside the examination hall/room.
10. Rough work is to be done on the space provided for this purpose in the Test Booklet only. This space is given at the bottom of each page and in 3 pages (Pages 21 – 23) at the end of the booklet.
11. On completion of the test, the candidate must hand over the Answer Sheet to the Invigilator on duty in the Room/Hall. However, the candidates are allowed to take away this Test Booklet with them.
12. The CODE for this Booklet is C. Make sure that the CODE printed on Side-2 of the Answer Sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
13. **Do not fold or make any stray marks on the Answer Sheet.**

PART-A : CHEMISTRY

1. The presence or absence of hydroxy group on which carbon atom of sugar differentiates RNA and DNA?
 (1) 1st (2) 2nd (3) 3^{er} (4) 4th

Ans. [2]

2. Among the following the maximum covalent character is shown by the compound
 (1) FeCl₂ (2) SnCl₂ (3) AlCl₃ (4) MgCl₂

Ans. [3]

3. Which of the following statements is wrong ?
 (1) The stability of hydrides increases from NH₃ to BiH₃ in group 15 of the periodic table.
 (2) Nitrogen cannot form dπ – pπ bond.
 (3) Single N – N bond is weaker than the single P – P bond.
 (4) N₂O₄ has two resonance structures

Ans. [1]

4. Phenol is heated with a solution of mixture of KBr and KBrO₃. The major product obtained in the above reaction is :
 (1) 2-Bromophenol (2) 3-Bromophenol (3) 4-Bromophenol (4) 2, 4, 6-Tribromophenol

Ans. [4]

5. A 5.2 molal aqueous solution of methyl alcohol, CH₃OH, is supplied. What is the mole fraction of methyl alcohol in the solution ?
 (1) 0.100 (2) 0.190 (3) 0.086 (4) 0.050

Ans. [3]

6. The hybridisation of orbitals of N atom in NO₃⁻, NO₂⁺ and NH₄⁺ are respectively
 (1) sp, sp², sp³ (2) sp², sp, sp³ (3) sp, sp³, sp² (4) sp², sp³, sp

Ans. [2]

7. Ethylene glycol is used as an antifreeze in a cold climate. Mass of ethylene glycol which should be added to 4 kg of water to prevent it from freezing at – 6° C will be (K_f for water = 1.86 K kg mol⁻¹, and molar mass of ethylene glycol mol⁻¹)
 (1) 804.32 g (2) 204.30 g (3) 400.00 g (4) 304.60 g

Ans. [1]

8. The reduction potential of hydrogen half-cell will be negative if
- (1) $p(\text{H}_2) = 1 \text{ atm}$ and $[\text{H}^+] = 2.0 \text{ M}$ (2) $p(\text{H}_2) = 1 \text{ atm}$ and $[\text{H}^+] = 1.0 \text{ M}$
 (3) $p(\text{H}_2) = 2 \text{ atm}$ and $[\text{H}^+] = 1.0 \text{ M}$ (4) $p(\text{H}_2) = 2 \text{ atm}$ and $[\text{H}^+] = 2.0 \text{ M}$

Ans. [3]

9. Which of the following reagents may be used to distinguish between phenol and benzoic acid ?
- (1) Aqueous NaOH (2) Tollen's reagent (3) Molisch reagent (4) Neutral FeCl_3

Ans. [4]

10. Trichloroacetaldehyde was subjected to Cannizzaro's reaction by using NaOH. The mixture of the products contains sodium trichloroacetate and another compound. The other compound is :
- (1) 2, 2, 2-Trichloroethanol (2) Trichloromethanol
 (3) 2, 2, 2-Trichloropropanol (4) Chloroform

Ans. [1]

11. Which one of the following ordered presents the correct sequence of the increasing basic nature of the given oxides ?
- (1) $\text{Al}_2\text{O}_3 < \text{MgO} < \text{Na}_2\text{O} < \text{K}_2\text{O}$ (2) $\text{MgO} < \text{K}_2\text{O} < \text{Al}_2\text{O}_3 < \text{Na}_2\text{O}$
 (3) $\text{Na}_2\text{O} < \text{K}_2\text{O} < \text{MgO} < \text{Al}_2\text{O}_3$ (4) $\text{K}_2\text{O} < \text{Na}_2\text{O} < \text{Al}_2\text{O}_3 < \text{MgO}$

Ans. [1]

12. A gas absorbs a photon of 355 nm and emits at two wavelengths. If one of the emissions is at 680 nm, the other is at :
- (1) 1035 nm (2) 325 nm (3) 743 nm (4) 518 nm

Ans. [3]

13. Which of the following statements regarding sulphur is incorrect ?
- (1) S_2 molecule is paramagnetic
 (2) The vapour at 200°C consists mostly
 (3) At 600°C the gas mainly consists of S_2 molecules
 (4) The oxidation state of sulphur is never less than + 4 in its compounds.

Ans. [4]

14. The entropy change involved in the isothermal reversible expansion of 2 moles of an ideal gas from a volume of 10 dm^3 to a volume of 100 dm^3 at 27°C is
- (1) $38.3 \text{ J mol}^{-2} \text{ K}^{-1}$ (2) $35.8 \text{ J mol}^{-1} \text{ K}^{-1}$ (3) $32.3 \text{ J mol}^{-1} \text{ K}^{-1}$ (4) $42.3 \text{ J mol}^{-1} \text{ K}^{-1}$

Ans. [1]

15. Which of the following facts about the complex $[\text{Cr}(\text{NH}_3)_6] \text{Cl}_3$ is wrong ?

- (1) The complex involves d^2sp^3 hybridisation and is octahedral in shape.
- (2) The complex is paramagnetic
- (3) The complex is an outer orbital complex.
- (4) The complex gives white precipitate with silver nitrate solution.

Ans. [3]

16. The structure of IF_7 is

- (1) square pyramid
- (2) trigonal bipyramid
- (3) octahedral
- (4) pentagonal bipyramid

Ans. [4]

17. The rate of a chemical reaction doubles for every 10°C rise of temperature. If the temperature is raised by 50°C , the rate of the reaction increases by about

- (1) 10 times
- (2) 24 times
- (3) 32 times
- (4) 64 times

Ans. [3]

18. The strongest acid amongst the following compounds is

- (1) CH_3COOH
- (2) HCOOH
- (3) $\text{CH}_3\text{CH}_2\text{CH}(\text{Cl})\text{CO}_2\text{H}$
- (4) $\text{ClCH}_2\text{CH}_2\text{CH}_2\text{COOH}$

Ans. [3]

19. Identify the compound that exhibits tautomerism.

- (1) 2-Butane
- (2) Lactic acid
- (3) 2-Pentanone
- (4) Phenol

Ans. [3]

20. A vessel at 1000 K contains CO_2 with a pressure of 0.5 atm. Some of the CO_2 is converted into CO on the addition of graphite. If the total pressure at equilibrium is 0.8 atm, the value of K is :

- (1) 1.8 atm
- (2) 3 atm
- (3) 0.3 atm
- (4) 0.18 atm

Ans. [1]

21. In context of the lanthanoids, which of the following statements is not correct ?

- (1) There is gradual decrease in the radii of the members with increasing atomic number in the series.
- (2) All the members exhibit + 3 oxidation state.
- (3) Because of similar properties the separation of lanthanoids is not easy.

(4) Availability of 4f electrons results in the formation of compounds in + 4 state for all the members of the series

Ans. [4]

22. a and b are van der Waal's constants for gases. Chlorine is more easily liquefied than ethane because :

- (1) a and b for $\text{Cl}_2 >$ a and b for C_2H_6
- (2) a and b for $\text{Cl}_2 <$ a and b C_2H_6
- (3) a for $\text{Cl}_2 <$ a for C_2H_6 but b for $\text{Cl}_2 >$ b for C_2H_6
- (4) a for $\text{Cl}_2 >$ a for C_2H_6 but b for $\text{Cl}_2 <$ b for C_2H_6

Ans. [4]

23. The magnetic moment (spin only) of $[\text{NiCl}_4]$ is :

- (1) 1.82 BM
- (2) 5.46 BM
- (3) 2.82 BM
- (4) 1.41 BM

Ans. [3]

24. In a face centered cubic lattice, atom A occupies the corner positions and atom B occupies the face centre positions. If one atom of B is missing from one of the face centered points, the formula of the compound is :

- (1) A_2B
- (2) AB_2
- (3) A_2B_3
- (4) A_2B_5

Ans. [4]

25. The outer electron configuration of Gd (Atomic N : 64) is :

- (1) $\text{af}^3 5\text{d}^5 6\text{s}^2$
- (2) $4\text{f}^8 5\text{d}^0 6\text{s}^2$
- (3) $4\text{f}^4 5\text{d}^4 6\text{s}^2$
- (4) $4\text{f}^7 5\text{d}^1 6\text{s}^2$

Ans. [4]

26. Boron cannot form which one of the following anions ?

- (1) BF_6^{3-}
- (2) BH_4^-
- (3) $\text{B}(\text{OH})_4^-$
- (4) BO_2^-

Ans. [1]

27. Ozonolysis of an organic compounds gives formaldehyde as one of the products. This confirms the presence of :

- (1) two ethylenic double bonds
- (2) a vinyl group
- (3) an isopropyl group
- (4) an acetylenic triple bond

Ans. [2]

28. Sodium ethoxide has reacted with ethanoyl chloride. The compound that is produced in the above reaction is :

- (1) Diethyl ether (2) 2-Butanone
(3) Ethyl chloride (4) Ethyl ethanoate

Ans. [4]

29. The degree of dissociation (α) of a weak electrolyte A_xB_y is related to van't Hoff factor (i) by the expression

- (1) $\alpha = \frac{i-1}{(x+y-1)}$ (2) $\alpha = \frac{i-1}{x+y+1}$ (3) $\alpha = \frac{x+y-1}{i-1}$ (4) $\alpha = \frac{x+y+1}{i-1}$

Ans. [1]

30. Silver Mirror test is given by which one of the following compounds ?

- (1) Acetaldehyde (2) Acetone (3) Formaldehyde (4) Benzophenone

Ans. [1, 3]

PART-B : PHYSICS

31. 100 g of water is heated from 30°C to 50°C. Ignoring the slight expansion of the water, the change in its internal energy is (specific heat of water is 4184 J/kg/K) :

(1) 4.2 kJ (2) 8.4 kJ (3) 84 kJ (4) 2.1 kJ

Ans. [2]

32. The half life of a radioactive substance is 20 minutes. The approximate time interval ($t_2 - t_1$) between the time t_2 when $\frac{2}{3}$ of it has decayed an time t_1 when $\frac{1}{3}$ of it had decayed is :

(1) 7 min (2) 14 min (3*) 20 min (4) 28 min

Ans. [3]

33. A mass M, attached to a horizontal spring, executes S.H.M. with amplitude A_1 . When the mass M passes through its mean position then a smaller mass m is placed over it and both of them move together with amplitude A_2 . The ratio of $\left(\frac{A_1}{A_2}\right)$ is :

(1) $\frac{M}{M+m}$ (2) $\frac{M+m}{M}$ (3) $\left(\frac{M}{M+m}\right)^{1/2}$ (4) $\left(\frac{M+m}{M}\right)^{1/2}$

Ans. [4]

34. Energy required for the electron excitation in Li^{++} from the first to the third Bohr orbit is :

(1) 12.1 eV (2) 36.3 eV (3*) 108.8 eV (4) 122.4 eV

Ans. [3]

35. The transverse displacement $y(x, t)$ of a wave on a string is given by

$$y(x, t) = e^{-(ax^2 + bt^2 + 2\sqrt{ab}xt)}$$

(1) wave moving in +x direction with speed (2) wave moving in -x direction with speed
(3) standing wave of frequency (4) standing wave of frequency

Ans. [2]

36. A resistor 'R' and $2\mu\text{F}$ capacitor in series is connected through a switch to 200V direct supply. Across the capacitor is a neon bulb that lights up at 120 V. Calculate the value of R to make the bulb light up 5s after the switch has been closed. ($\log_{10} 2.5 = 0.4$)

(1) $1.3 \times 10^4 \Omega$ (2) $1.7 \times 10^5 \Omega$ (3) $2.7 \times 10^6 \Omega$ (4) $3.3 \times 10^7 \Omega$

Ans. [3]

37. A current I flows in an infinitely long wire with cross section in the form of a semi-circular ring of radius R . The magnitude of the magnetic induction along its axis is :

(1) $\frac{\mu_0 I}{\pi^2 R}$ (2) $\frac{\mu_0 I}{2\pi^2 R}$ (3) $\frac{\mu_0 I}{2\pi R}$ (4) $\frac{\mu_0 I}{4\pi R}$

Ans. [1]

38. A Carnot engine operating between temperatures T_1 and T_2 has efficiency $\frac{1}{6}$. When T_2 is lowered by 62 K ; its efficiency increases to $\frac{1}{3}$. Then T_1 and T_2 are respectively :

(1) 372 K and 310 K (2) 372 K and 330 K (3) 330 K and 268 K (4) 310 K and 248 K

Ans. [1]

39. An object, moving with a speed of 6.25 m/s, is decelerated at a rate given by

$$\frac{dv}{dt} = -2.5\sqrt{v}$$

where v is the instantaneous speed. The time taken by the object, to come to rest, would be :

(1) 1s (2) 2s (3) 4s (4) 8s

Ans. [2]

40. The electrostatic potential inside a charged spherical ball is given by $\phi = ar^2 + b$ where r is the distance from the centre ; a, b are constant. Then the charge density inside the ball is :

(1) $-24\pi a\epsilon_0 r$ (2) $-6 a\epsilon_0 r$ (3) $-24\pi a\epsilon_0$ (4) $-6 a\epsilon_0$

Ans. [4]

41. A car is fitted with a convex side-view mirror of focal length 20 cm. A second car 2.8 m behind the first car is overtaking the first car at a relative speed of 15 m/s. The speed of the image of the second car as seen in the mirror of the first one is :

(1) $\frac{1}{10}$ m/s (2) $\frac{1}{15}$ m/s (3) 10 m/s (4) 15 m/s

Ans. [2]

42. If a wire is stretched to make it 0.1% longer, its resistance will :

(1) increase by 0.05% (2) increase by 0.2%
(3) decrease by 0.2% (4) decrease by 0.05%

Ans. [2]

43. Three perfect gases at absolute temperatures T_1 , T_2 and T_3 are mixed. The masses of molecules are m_1 , m_2 and m_3 and the number of molecules are n_1 , n_2 and n_3 respectively. Assuming no loss of energy, the final temperature of the mixture is :

$$(1) \frac{(T_1 + T_2 + T_3)}{3} \quad (2) \frac{n_1 T_1 + n_2 T_2 + n_3 T_3}{n_1 + n_2 + n_3}$$

$$(3) \frac{n_1 T_1^2 + n_2 T_2^2 + n_3 T_3^2}{n_1 T_1 + n_2 T_2 + n_3 T_3} \quad (4) \frac{n_1^2 T_1^2 + n_2^2 T_2^2 + n_3^2 T_3^2}{n_1 T_1 + n_2 T_2 + n_3 T_3}$$

Ans. [2]

44. Two identical charged spheres suspended from a common point by two massless strings of length ℓ are initially a distance d ($d \ll \ell$) apart because of their mutual repulsion. The charge begins to leak from both the spheres at a constant rate. As a result the charges approach each other with a velocity v . Then as a function of distance x between them,

$$(1) v \propto x^{-1/2} \quad (2) v \propto x^{-1} \quad (3) v \propto x^{1/2} \quad (4) v \propto x$$

Ans. [1]

45. Work done in increasing the size of a soap bubble from a radius of 3 cm to 5 cm is nearly (surface tension of soap solution = 0.03 Nm^{-1}) :

$$(1) 4 \pi \text{ mJ} \quad (2) 0.2 \pi \text{ mJ} \quad (3) 2 \pi \text{ mJ} \quad (4) 0.4 \pi \text{ mJ}$$

Ans. [4]

46. A fully charged capacitor C with initial charge q_0 is connected to a coil of self inductance L at $t = 0$. The time at which the energy is stored equally between the electric and magnetic fields is :

$$(1) \pi\sqrt{LC} \quad (2) \frac{\pi}{4}\sqrt{LC} \quad (3) 2\pi\sqrt{LC} \quad (4) \sqrt{LC}$$

Ans. [2]

47. Two bodies of masses m and $4m$ are placed at a distance r . The gravitational potential at a point on the line joining them where the gravitational field is zero is :

$$(1) \text{zero} \quad (2) -\frac{4Gm}{r} \quad (3) -\frac{6Gm}{r} \quad (4) -\frac{9Gm}{r}$$

Ans. [4]

48. A thin horizontal circular disc is rotating about a vertical axis passing through its centre. An insect is at rest at a point near the rim of the disc. The insect now moves along a diameter of the disc to reach its other end. During the journey of the insect, the angular speed of the disc:

$$(1) \text{remains unchanged} \quad (2) \text{continuously decreases}$$

$$(3) \text{continuously increases} \quad (4) \text{first increases and then decreases}$$

Ans. [4]

49. Let the $x - z$ plane be the boundary between two transparent media. Medium 1 in $z \geq 0$ has a refractive index of $\sqrt{2}$ and medium 2 with $z < 0$ has a refractive index of $\sqrt{3}$. A ray of light in medium 1 given by the vector $\vec{A} = 6\sqrt{3}\hat{i} + 8\sqrt{3}\hat{j} - 10\hat{k}$ is incident on the plane of separation. The angle of refraction in medium 2 is :

- (1) 30° (2) 45° (3) 60° (4) 75°

Ans. [2]

50. Two particles are executing simple harmonic motion of the same amplitude A and frequency ω along the x -axis. Their mean position is separated by distance X_0 ($X_0 > A$). If the maximum separation between them is $(X_0 + A)$, the phase difference between their motion is :

- (1) $\frac{\pi}{2}$ (2) $\frac{\pi}{3}$ (3) $\frac{\pi}{4}$ (4) $\frac{\pi}{6}$

Ans. [2]

51. **Direction :**

The question has a paragraph followed by two statements, **Statement-1** and **Statement-2**. Of the given four alternatives after the statements, choose the one that describes the statements.

A thin air film is formed by putting the convex surface of a plane-convex lens over a plane glass plate. With monochromatic light, this film gives an interference pattern due to light reflected from the top (Convex) surface and the bottom (glass plate) surface of the film.

Statement-1 : When light reflects from the air-glass plate interface, the reflected wave suffers a phase change of π

Statement-2 : The centre of the interference pattern is dark.

- (1) Statement-1 is true, Statement-2 is false
 (2) Statement-1 is true, Statement-2 is true and Statement -2 is the correct explanation of Statement-1.
 (3) Statement-1 is true, Statement-2 is true and Statement-2 is **not** the correct explanation of Statement-1
 (4) Statement-1 is false, Statement-2 is true.

Ans. [3]

52. The thermally insulated vessel contains an ideal gas of molecular mass M and ratio of specific heat γ . It is moving with speed v and is suddenly brought to rest. Assuming no heat is lost to the surroundings, its temperature increases by :

- (1) $\frac{(\gamma - 1)}{2(\gamma + 1)R} Mv^2 K$ (2) $\frac{(\gamma - 1)}{2\gamma R} Mv^2 K$
 (3) $\frac{\gamma Mv^2}{2R} K$ (4) $\frac{(\gamma - 1)}{2R} Mv^2 K$

Ans. [4]

53. A screw gauge gives the following reading when used to measure the diameter of a wire.

Main scale reading : 0 mm.

Circular scale reading : 52 divisions

Given that 1 mm on main scale corresponds to 100 divisions of the circular scale. The diameter of wire from the above data is :

- (1) 0.52 cm (2) 0.052 cm (3) 0.026 cm (4) 0.005 cm

Ans. [2]

54. A boat is moving due east in a region where the earth's magnetic field is $5.0 \times 10^{-5} \text{ NA}^{-1} \text{ m}^{-1}$ due north and horizontal. The boat carries a vertical aerial 2m long. If the speed of the boat is 1.50 ms^{-1} , the magnitude of the induced emf in the wire of aerial is :

- (1) 1 mV (2) 0.75 mV (3) 0.50 mV (4) 0.15 mV

Ans. [4]

55. This question has Statement-1 and Statement-2. Of the four choices given after the statements, choose the one that best describes the two statements.

Statement-1 : Sky wave signals are used for long distance radio communication. These signals are in general, less stable than ground wave signals.

Statement -2 : The state of ionosphere varies from hour to hour, day to day and season to season.

- (1) Statement-1 is true, Statement-2 is false
 (2) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.
 (3) Statement-1 is true, Statement-2 is true and Statement-2 is **not** the correct explanation of Statement-1
 (4) Statement-1 is false, Statement-2 is true.

Ans. [2]

56. A mass m hangs with the help of a string wrapped around a pulley on a frictionless bearing. The pulley has mass m and radius R . Assuming pulley to be a perfect uniform circular disc, the acceleration of the mass m , if the string does not slip on the pulley, is :

- (1) $\frac{3}{2}g$ (2) g (3) $\frac{2}{3}g$ (4) $\frac{g}{3}$

Ans. [3]

57. A water fountain on the ground sprinkles water all around it. If the speed of water coming out of the fountain is v , the total area around the fountain that gets wet is :

- (1) $\pi \frac{v^2}{g}$ (2) $\pi \frac{v^4}{g^2}$ (3) $\frac{\pi v^4}{2 g^2}$ (4) $\pi \frac{v^2}{g^2}$

Ans. [2]

58. This question has Statement-1 and Statement-2. Of the four choices given after the statements, choose the one that best describes the two statements.

Statement-1 : A metallic surface is irradiated by a monochromatic light of frequency $\nu > \nu_0$ (the threshold frequency). The maximum kinetic energy and the stopping potential are $K_{\max}$ and V_0 respectively. If the frequency incident on the surface is doubled, both the $K_{\max}$ and V_0 are also doubled.

Statement -2 : The maximum kinetic energy and the stopping potential of photoelectrons emitted from a surface are linearly dependent on the frequency of incident light.

- (1) Statement-1 is true, Statement-2 is false
(2) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.
(3) Statement-1 is true, Statement-2 is true and Statement-2 is **not** the correct explanation of Statement-1
(4) Statement-1 is false, Statement-2 is true.

Ans. [4]

59. A pulley of radius 2m is rotated about its axis by a force $F = (20t - 5t^2)$ newton (where t is measured in seconds) applied tangentially. If the moment of inertia of the pulley about its axis of rotation is 10 kg m^2 , the number of rotations made by the pulley before its direction of motion if reversed, is :

- (1) less than 3 (2) more than 3 but less than 6
(3) more than 6 but less than 9 (4) more than 9

Ans. [2]

60. Water is flowing continuously from a tap having an internal diameter $8 \times 10^{-3} \text{ m}$. The water velocity as it leaves the tap is 0.4 ms^{-1} . The diameter of the water stream at a distance $2 \times 10^{-1} \text{ m}$ below the tap is close to :

- (1) $5.0 \times 10^{-3} \text{ m}$ (2) $7.5 \times 10^{-3} \text{ m}$ (3) $9.6 \times 10^{-3} \text{ m}$ (4) $3.6 \times 10^{-3} \text{ m}$

Ans. [4]

PART-C : MATHEMATICS

61. Let α, β be real and z be complex number. If $z^2 + \alpha z + \beta = 0$ has two distinct roots on the line $\operatorname{Re} z = 1$, then it is necessary that :

- (1) $\beta \in (0, 1)$ (2) $\beta \in (-1, 0)$ (3) $|\beta| = 1$ (4) $\beta \in (1, \infty)$

Ans. [4]

62. The value of $\int_0^1 \frac{8 \log(1+x)}{1+x^2} dx$ is :

- (1) $\pi \log 2$ (2) $\frac{\pi}{8} \log 2$ (3) $\frac{\pi}{2} \log 2$ (4) $\log 2$

Ans. [1]

63. $\frac{d^2x}{dy^2}$ equals :

- (1) $\left(\frac{d^2y}{dx^2}\right)^{-1}$ (2) $-\left(\frac{d^2y}{dx^2}\right)^{-1} \left(\frac{dy}{dx}\right)^{-3}$ (3) $\left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-2}$ (4) $-\left(\frac{d^2y}{dx^2}\right) \left(\frac{dy}{dx}\right)^{-3}$

Ans. [4]

64. Let I be the purchase value of an equipment and $V(t)$ be the value after it has been used for t years. The value $V(t)$ depreciates at a rate given by differential equation $\frac{dV(t)}{dt} = -k(T - t)$, where $k > 0$ is a constant and T is the total life in years of the equipment. Then the scrap value $V(T)$ of the equipment is :

- (1) $T^2 - \frac{I}{k}$ (2) $I - \frac{kT^2}{2}$ (3) $I - \frac{k(T-t)^2}{2}$ (4) $e - kT$

Ans. [2]

65. The coefficient of x^7 in the expansion of $(1 - x - x^2 + x^3)^6$ is :

- (1) 144 (2) -132 (3) -144 (4) 132

Ans. [3]

66. For $x \in \left(0, \frac{5\pi}{2}\right)$, define $f(x) = \int_0^x \sqrt{t} \sin t \, dt$. Then f has

- (1) local maximum at π and 2π
 (2) local maximum at π and 2π
 (3) local maximum at π and local maximum at 2π
 (4) local maximum at π and local minimum at 2π

Ans. [4]

67. The area of the region enclosed by the curves $y = x$, $x = e$, $y = 1/x$ and the positive x-axis is :

- (1) $1/2$ square units (2) 1 square units
(3) $3/2$ square units (4) $5/2$ square units

Ans. [3]

68. The lines $L_1 : y - x = 0$ and $L_2 : 2x + y = 0$ intersect the line $L_3 : y + 2 = 0$ at P and Q respectively. The bisector of the acute between L_1 and L_2 intersects L_3 at R.

Statement-1 : The ratio PR : RQ equals $2\sqrt{2} : \sqrt{5}$

Statement -2 : In any triangle, bisector of an angle divides the triangle into two similar triangle.

- (1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.
(2) Statement-1 is true, Statement-2 is false and Statement-2 is **not** the correct explanation of Statement-1
(3) Statement-1 is true, Statement-2 is false
(4) Statement-1 is false, Statement-2 is true.

Ans. [3]

69. The value of p and q for which the function $f(x) = \begin{cases} \frac{\sin(p+1)x \sin x}{x}, & x < 0 \\ q, & x = 0 \\ \frac{\sqrt{x+x^2} - \sqrt{x}}{x^{3/2}}, & x > 0 \end{cases}$ is continuous for all x in R, are:

- (1) $p = \frac{1}{2}, q = -\frac{3}{2}$ (2) $p = \frac{5}{2}, q = \frac{1}{2}$ (3) $p = -\frac{3}{2}, q = \frac{1}{2}$ (4) $p = \frac{1}{2}, q = \frac{3}{2}$

Ans. [3]

70. If the angle between the line $x = \frac{y-1}{2} = \frac{z-3}{\lambda}$ and the plane $x + 2y + 3z = 4$ is $\cos^{-1} \left(\sqrt{\frac{5}{14}} \right)$, then λ equals :

- (1) $2/3$ (2) $3/2$ (3) $2/5$ (4) $5/2$

Ans. [1]

71. The domain of the function $f(x) = \frac{1}{\sqrt{|x| - x}}$ is :

- (1) $(-\infty, \infty)$ (2) $(0, \infty)$ (3) $(-\infty, 0)$ (4) $(-\infty, \infty) - \{0\}$

Ans. [3]

72. The shortest distance between line $y - x = 1$ and curve $x = y^2$ is :

- (1) $\frac{\sqrt{3}}{4}$ (2) $\frac{3\sqrt{2}}{8}$ (3) $\frac{8}{3\sqrt{2}}$ (4) $\frac{4}{\sqrt{3}}$

Ans. [2]

73. A man saves Rs. 200 in each of the first three months of his service. In each of the subsequent months of his service. In each of the subsequent months his saving increases by Rs. 40 more than the saving of immediately previous month. His total saving from the start of service will be Rs. 11040 after.

(1) 18 months (2) 19 months (3) 20 months (4) 21 months

Ans. [4]

74. Consider the following statements

P : Suman is brilliant

Q : Suman is rich

R : Suman is honest

The negation of the statement "Suman is brilliant and dishonest if and only if Suman is rich" can be expressed as :

(1) $\sim P \wedge (Q \leftrightarrow R)$ (2) $\sim (Q \leftrightarrow (P \wedge \sim R))$ (3) $\sim Q \leftrightarrow \sim P \wedge$ (4) $\sim (P \wedge \sim R) \leftrightarrow Q$

Ans. [2,4]

75. If $\omega (\neq 1)$ is a cube root of unit, and $(1 + \omega)^7 = A = B\omega$. Then (A, B) equals :

(1) (0, 1) (2) (1, 1) (3) (2, 0) (4) (-1, 1)

Ans. [2]

76. If $\vec{a} = \frac{1}{\sqrt{10}}(3\hat{i} + \hat{k})$ and $\vec{b} = \frac{1}{7}(2\hat{i} + 3\hat{j} - 6\hat{k})$, then the value of $(2\vec{a} - \vec{b}) \cdot [(\vec{a} \times \vec{b}) \times (\vec{a} + 2\vec{b})]$ is :

(1) -5 (2) -3 (3) 5 (4) 3

Ans. [1]

77. If $\frac{dy}{dx} = y + 3 > 0$ and $y(0) = 2$, then $y(\ln 2)$ is equal to :

(1) 7 (2) 5 (3) 13 (4) -2

Ans. [1]

78. Equation of the ellipse whose axis are the axis of coordinates and which passes through the point $(-3, 1)$ and has eccentricity $\sqrt{\frac{2}{5}}$ is :

(1) $3x^2 + 5y^2 - 32 = 0$ (2) $5x^2 + 3y^2 - 48 = 0$
(3) $3x^2 + 5y^2 - 15 = 0$ (4) $5x^2 + 3y^2 - 32 = 0$

Ans. [1,2]

79. If the mean deviation about the median of the numbers $a, 2a, \dots, 50a$ is 50, then $|a|$ equals :

(1) 2 (2) 3 (3) 4 (4) 6

Ans. [3]

80. $\lim_{x \rightarrow 2} \left(\frac{\sqrt{1 - \cos\{2(x-2)\}}}{x-2} \right)$

(1) does not exist

(2) equals $\sqrt{2}$

(3) equals $-\sqrt{2}$

(4) equals $\frac{1}{\sqrt{2}}$

Ans. [1]

81. **Statement-1** : The number of ways of distributing 10 identical balls in 4 distinct boxes such that no box is empty is 9C_3 .

Statement -2 : The number of ways of choosing any 3 places from 9 different places is 9C_3 .

(1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.

(2) Statement-1 is true, Statement-2 is false and Statement-2 is **not** the correct explanation of Statement-1

(3) Statement-1 is true, Statement-2 is false

(4) Statement-1 is false, Statement-2 is true.

Ans. [1]

82. Let R be the set of real numbers.

Statement-1 : $A = \{(x, y) \in R \times R : y - x \text{ is an integer}\}$ is an equivalence relation on R .

Statement-2 : $B = \{(x, y) \in R \times R : x = \alpha y \text{ for some rational number } \alpha\}$ is an equivalence relation on R .

(1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.

(2) Statement-1 is true, Statement-2 is false and Statement-2 is **not** the correct explanation of Statement-1

(3) Statement-1 is true, Statement-2 is false

(4) Statement-1 is false, Statement-2 is true.

Ans. [3]

83. Consider 5 independent Bernoulli's trials each with probability of success p . If the probability of at least one failure is greater than or equal to $\frac{31}{32}$, then p lies in the interval :

(1) $\left[\frac{1}{2}, \frac{3}{4}\right]$

(2) $\left[\frac{3}{4}, \frac{11}{12}\right]$

(3) $\left[0, \frac{1}{2}\right]$

(4) $\left[\frac{11}{12}, 1\right]$

Ans. [3]

84. The two circles $x^2 + y^2 = ax$ and $x^2 + y^2 = c^2$ ($c > 0$) touch each other if

(1) $2|a| = c$

(2) $|a| = c$

(3) $a = 2c$

(4) $|a| = 2c$

Ans. [2]

85. Let A and B be two symmetric matrices of order 3.

Statement-1 : $A(BA)$ and $(AB)A$ are symmetric matrices.

Statement-2 : AB is symmetric matrix if matrix multiplication of A with B is commutative.

- (1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.
 (2) Statement-1 is true, Statement-2 is false and Statement-2 is **not** the correct explanation of Statement-1
 (3) Statement-1 is true, Statement-2 is false
 (4) Statement-1 is false, Statement-2 is true.

Ans. [2]

86. If C and D are two events such that $C \subset D$ and $P(D) \neq 0$, then the correct statement among the following is :

- (1) $P(C | D) = P(C)$ (2) $P(C | D) \geq P(C)$ (3) $P(C | D) < P(C)$ (4) $P(C | D) = \frac{P(D)}{P(C)}$

Ans. [2]

87. The vectors $\vec{a}$ and $\vec{b}$ are not perpendicular and $\vec{c}$ and $\vec{d}$ are two vector satisfying :

$\vec{b} \times \vec{c} = \vec{b} \times \vec{d}$ and $\vec{a} \cdot \vec{d} = 0$. Then the vector $\vec{d}$ is equal to :

- (1) $\vec{b} - \left(\frac{\vec{b} \cdot \vec{c}}{\vec{a} \cdot \vec{b}} \right) \vec{c}$ (2) $\vec{c} + \left(\frac{\vec{a} \cdot \vec{c}}{\vec{a} \cdot \vec{b}} \right) \vec{b}$ (3) $\vec{b} + \left(\frac{\vec{b} \cdot \vec{c}}{\vec{a} \cdot \vec{b}} \right) \vec{c}$ (4) $\vec{c} - \left(\frac{\vec{a} \cdot \vec{c}}{\vec{a} \cdot \vec{b}} \right) \vec{b}$

Ans. [4]

88. **Statement-1 :** The point A(1, 0, 7) is the mirror image of the point B (1, 6, 3) in the line $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$

Statement 2 : The line : $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$ bisects the line segment joining A(1, 0, 7) and B(1, 6, 3).

- (1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.
 (2) Statement-1 is true, Statement-2 is false and Statement-2 is **not** the correct explanation of Statement-1
 (3) Statement-1 is true, Statement-2 is false
 (4) Statement-1 is false, Statement-2 is true.

Ans. [2]

89. If $A = \sin^2 x + \cos^4 x$, then for all real x :

- (1) $\frac{3}{4} \leq A \leq 1$ (2) $\frac{13}{16} \leq A \leq 1$ (3) $1 \leq A \leq 2$ (4) $\frac{3}{4} \leq A \leq \frac{13}{16}$

Ans. [1]

90. The number of values of k for which the linear equations

$$4x + ky + 2z = 0$$

$$kx + 4y + z = 0$$

$$2x + 2y + z = 0$$

posses a non-zero solution is :

- (1) 3 (2) 2 (3) 1 (4) zero

Ans. [2]