

**JEE MAINS-2014****ONLINE 19-04-2014****IMPORTANT INSTRUCTIONS**

1. Immediately fill in the particulars on this page of the Test Booklet with **Blue/Black Ball Point Pen**. **Use of pencil is strictly prohibited.**
2. The test is of **3** hours duration.
3. The Test Booklet consists of **90** questions. The maximum marks are **360**.
4. There are **three** parts in the question paper A, B, C consisting of **Physics, Chemistry and Mathematics** having 30 questions in each part of equal weightage. Each question is allotted **4 (four)** marks for each correct response.
5. Candidates will be awarded marks as stated above in instruction No.5 for correct response of each question. 1/4 (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
6. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 5 above.

PART-A-PHYSICS

1. Match List - I (Event) with List - II (order of the time interval for happening of the event) and select the correct option from the options given below the lists

List - I	List - II
(a) Rotation period of earth	(i) 10^5 s
(b) Revolution period of earth	(ii) 10^7 s
(c) Period of a light wave	(iii) 10^{-15} s
(d) Period of a sound wave	(iv) 10^{-3} s
(1*) (a) - (i), (b) - (ii), (c) - (iii), (d) - (iv)	(2) (a) - (ii), (b) - (i), (c) - (iv), (d) - (iii)
(3) (a) - (i), (b) - (ii), (c) - (iv), (d) - (iii)	(4) (a) - (ii), (b) - (i), (c) - (iii), (d) - (iv)

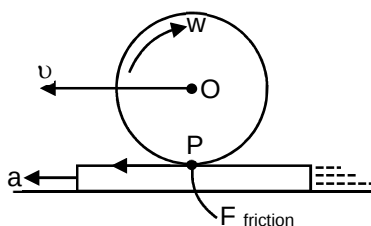
2. A bullet loses $\left(\frac{1}{n}\right)^{\text{th}}$ of its velocity passing through one plank. The number of such planks that are required to stop the bullet can be:

(1*) $\frac{n^2}{2n-1}$ (2) $\frac{2n^2}{n-1}$ (3) Infinite (4) n

3. A heavy box is to be dragged along a rough horizontal floor. To do so, person A pushes it at an angle 30° from the horizontal and requires a minimum force F_A . While person B pulls the box at an angle 60° from the horizontal and needs minimum force F_B . If the coefficient of friction between the box and the floor is, $\frac{\sqrt{3}}{5}$ the ratio $\frac{F_A}{F_B}$ is:

(1) $\sqrt{3}$ (2) $\frac{5}{\sqrt{3}}$ (3) $\sqrt{\frac{3}{2}}$ (4*) $\frac{2}{\sqrt{3}}$

4. Consider a cylinder of mass M resting on a rough horizontal rug that is pulled out from under it with acceleration 'a' perpendicular to the axis of the cylinder. What is F_{friction} at point P? It is assumed that the cylinder does not slip.



(1) Mg (2) Ma (3) $\frac{Ma}{2}$ (4*) $\frac{Ma}{3}$

5. A particle is released on a vertical smooth semicircular track from point X so that OX makes angle θ from the vertical (see figure). The normal reaction of the track on the particle vanishes at point Y where OY makes angle ϕ with the horizontal. Then:

(1) $\sin \phi = \cos \theta$ (2) $\sin \phi = \frac{1}{2} \cos \theta$ (3*) $\sin \phi = \frac{2}{3} \cos \theta$ (4) $\sin \phi = \frac{3}{4} \cos \theta$

6. A ball of mass 160 g is thrown up at an angle of 60° to the horizontal at a speed of 10 ms^{-1} . The angular momentum of the ball at the highest point of the trajectory with respect to the point from which the ball is thrown is nearly

($g = 10 \text{ ms}^{-2}$)

(1) $1.73 \text{ kg m}^2/\text{s}$ (2*) $3.0 \text{ kg m}^2/\text{s}$ (3) $3.46 \text{ kg m}^2/\text{s}$ (4) $6.0 \text{ kg m}^2/\text{s}$

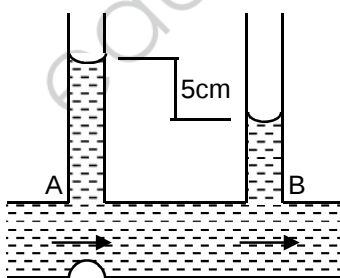
7. The gravitational field in a region is given by $\vec{g} = 5\text{N/kg}\hat{i} + 12\text{N/kg}\hat{j}$. The change in the gravitational potential energy of particle of mass 2 kg when it is taken from the origin to a point (7m, -3m) is:

(1) 71 J (2) $13\sqrt{58}\text{J}$ (3) -71 J (4) 1 J

8. The velocity of water in a river is 18 km/hr near the surface. If the river is 5m deep, find the shearing stress between the horizontal layers of water. The co-efficient of water = 10^{-2} poise.

(1) 10^{-1} N/m^2 (2) 10^{-2} N/m^2 (3) 10^{-3} N/m^2 (4) 10^{-4} N/m^2

9. In the diagram shown, the difference in the two tubes of the manometer is 5 cm, the cross section of the tube at A and B is 6mm^2 and 10 mm^2 respectively. The rate at which water flows through the tube is ($g = 10 \text{ ms}^{-2}$)



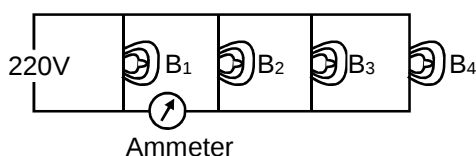
(1*) 7.5 cc/s (2) 8.0 cc/s (3) 10.0 cc/s (4) 12.5 cc/s

10. A large number of liquid drops each of radius r coalesce to form a single drop of radius R . The energy released in the process is converted into kinetic energy of the big drop so formed. The speed of the big drop is (given surface tension of liquid T , density ρ)

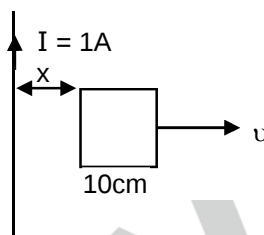
(1) $\sqrt{\frac{T}{\rho} \left(\frac{1}{r} - \frac{1}{R} \right)}$ (2) $\sqrt{\frac{2T}{\rho} \left(\frac{1}{r} - \frac{1}{R} \right)}$ (3) $\sqrt{\frac{4T}{\rho} \left(\frac{1}{r} - \frac{1}{R} \right)}$ (4*) $\sqrt{\frac{6T}{\rho} \left(\frac{1}{r} - \frac{1}{R} \right)}$

11. A black coloured solid sphere of radius R and mass M is inside a cavity with vacuum inside. The walls of the cavity are maintained at temperature T_0 . The initial temperature of the sphere is $3T_0$. If the specific heat of the material of the sphere varies as αT^3 per unit mass with the temperature T of the sphere where α is a constant then the time taken for the sphere to cool down to temperature $2T_0$ will be (σ is stefan Boltzmann constant)
- (1) $\frac{M\alpha}{4\pi R^2\sigma} \ln\left(\frac{3}{2}\right)$ (2) $\frac{M\alpha}{4\pi R^2\sigma} \ln\left(\frac{16}{3}\right)$ (3*) $\frac{M\alpha}{16\pi R^2\sigma} \ln\left(\frac{16}{3}\right)$ (4) $\frac{M\alpha}{16\pi R^2\sigma} \ln\left(\frac{3}{2}\right)$
12. A gas is compressed from a volume of 2 m^3 to a volume of 1 m^3 at a constant pressure of 100 N/m^2 . Then it is heated at constant volume by supplying 150 J of energy. As a result, the internal energy of the gas:
- (1) Increases by 250 J (2) Decreases by 250 J
 (3) Increases by 50 J (4) Decreases by 50 J
13. A gas molecule of mass M at the surface of the Earth has kinetic energy equivalent to 0°C . If it were to go up straight without colliding with any other molecules, how high it would rise? Assume that the height attained is much less than radius of the earth. (k_B is Boltzmann constant)
- (1) 0 (2) $\frac{273k_B}{2Mg}$ (3) $\frac{546k_B}{3Mg}$ (4*) $\frac{819k_B}{2Mg}$
14. A body is in simple harmonic motion with time period half second ($T = 0.5 \text{ s}$) and amplitude one cm ($A = 1 \text{ cm}$). Find the average velocity in the interval in which it moves from equilibrium position to half of its amplitude.
- (1) 4 cm/s (2) 6 cm/s (3*) 12 cm/s (4) 16 cm/s
15. The total length of a sonometer wire between fixed ends is 110cm . Two bridges are placed to divide the length of wire in ratio $6 : 3 : 2$. The tension in the wire is 400 N and the mass per unit length is 0.01 kg/m . What is the minimum common frequency with which three parts can vibrate?
- (1) 1100 Hz (2*) 1000 Hz (3) 166 Hz (4) 100 Hz
16. The electric field in a region of space is given by $\vec{E} = E_0\hat{i} + 2E_0\hat{j}$ where $E_0 = 100\text{N/C}$. The flux of this field through a circular surface of radius 0.02 m parallel to the $Y-Z$ plane is nearly
- (1) $0.125 \text{ Nm}^2/\text{C}$ (2) $0.02 \text{ Nm}^2/\text{C}$ (3) $0.005 \text{ Nm}^2/\text{C}$ (4) $3.14 \text{ Nm}^2/\text{C}$
17. The gap between the plates of a parallel plate capacitor of area A and distance between plates d , is filled with a dielectric whose permittivity varies linearly from ϵ_1 at one plate to ϵ_2 at the other. The capacitance of capacitor is:
- (1) $\epsilon_0 (\epsilon_1 + \epsilon_2) A / d$ (2) $\epsilon_0 (\epsilon_2 + \epsilon_1) A / 2d$
 (3) $\epsilon_0 A / [\ln(\epsilon_2 / \epsilon_1)]$ (4*) $\epsilon_0 (\epsilon_2 - \epsilon_1) A / [d \ln(\epsilon_2 / \epsilon_1)]$

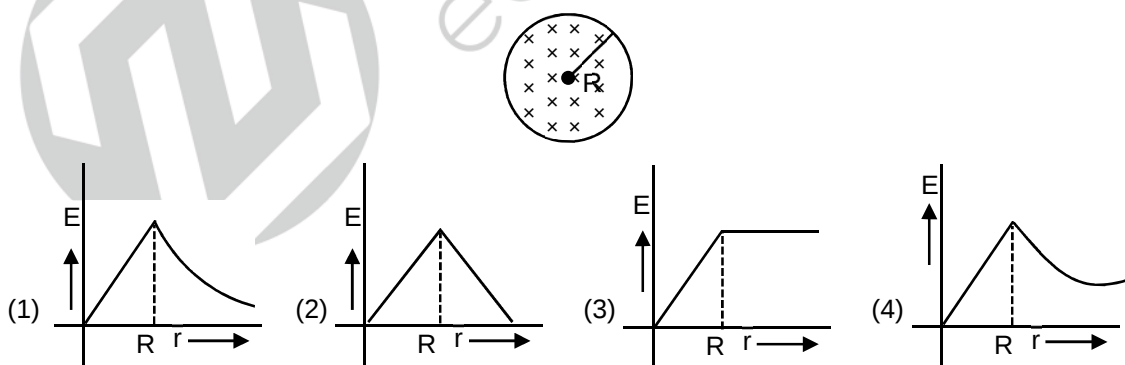
18. Four bulbs B_1 , B_2 , B_3 and B_4 of 100 W each are connected to 220 V main as shown in the figure. The reading in an ideal ammeter will be:



19. A square frame of side 10 cm and a long straight wire carrying current 1A are in the plane of the paper. Starting from close to the wire, the frame moves towards the right with a constant speed of 10 ms^{-1} (see figure). The e.m.f induced at the time the left arm of the frame is at $x = 10 \text{ cm}$ from the wire is:



20. An example of a perfect diamagnet is a super conductor. This implies that when a superconductor is put in a magnetic field of intensity B , the magnetic field B_s inside the superconductor will be such that:
21. Figure shows a circular area of radius R where a uniform magnetic field $\vec{B}$ is going into the plane of paper and increasing in magnitude at a constant rate. In that case, which of the following graphs, drawn schematically, correctly shows the variation of the induced electric field $E(r)$?



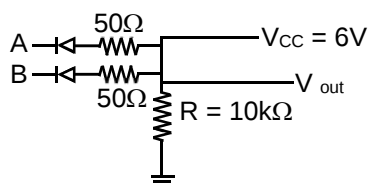
22. If denote microwaves, X rays, infrared, gamma rays, ultra-violet, radio waves and visible parts of the electromagnetic spectrum by M, X, I, G, U, R and V, the following is the arrangement in ascending order of wavelength:

23. A ray of light is incident from a denser to a rarer medium. The critical angle for total internal reflection is θ_{iC} and the Brewster's angle of incidence is θ_{iB} , such that $\sin\theta_{iC}/\sin\theta_{iB} = \eta = 1.28$. The relative refractive index of the two media is:
 (1) 0.2 (2) 0.4 (3*) 0.8 (4) 0.9
24. The diameter of the objective lens of microscope makes an angle β at the focus of the microscope. Further, the medium between the object and the lens is an oil of refractive index n . Then the resolving power of the microscope.
 (1) Increases with decreasing value of n
 (2) Increases with decreasing value of β
 (3*) increases with increasing value of $n \sin 2\beta$
 (4) Increases with increasing value of $\frac{1}{n \sin 2\beta}$
25. In a Young's double slit experiment, the distance between the two identical slits is 6.1 times larger than the slit width. Then the number of intensity maxima observed within the central maximum of the single slit diffraction pattern is:
 (1) 3 (2) 6 (3*) 12 (4) 24
26. Match List - I (Experiment performed) with List - II (phenomena discovered) associated and select the correct option from the options given below the lists:
 List - I List - II
 (a) Davisson and Germer Experiment (i) Wave nature of electrons
 (b) Milikan's oil drop experiment (ii) Charge of an electron
 (c) Rutherford experiment (iii) Quantisation of energy levels
 (d) Franck-Hertz experiment (iv) Existence of nucleus
 (1) (a) - (i), (b) - (ii), (c) - (iii), (d) - (iv)
 (2*) (a) - (i), (b) - (ii), (c) - (iv), (d) - (iii)
 (3) (a) - (iii), (b) - (iv), (c) - (i), (d) - (ii)
 (4) (a) - (iv), (b) - (iii), (c) - (ii), (d) - (i)
27. A piece of wood from a recently cut tree shows 20 decays per minute. A wooden piece of same size placed in a museum (obtained from a tree cut many years back) shows 2 decays per minute. If half life of C^{14} is 5730 years, then age of the wooden piece placed in the museum is approximately:
 (1) 10439 years (2) 13094 years
 (3*) 19039 years (4) 39049 years

28. Given: A and B are input terminals

Logic 1 = $> 5V$

Logic 0 = $< 1V$



Which logic gate operation, the following circuit does?

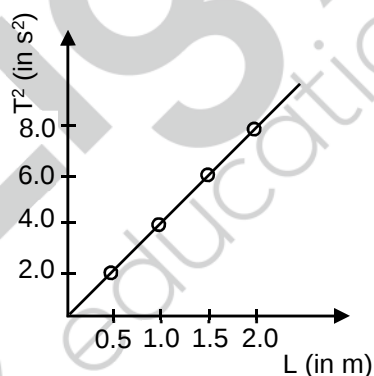
- (1*) AND Gate (2) OR Gate (3) XOR Gate (4) NOR Gate

29. Long range radio transmission is possible when the radiowaves are reflected from the ionosphere. For this to happen the frequency of the radiowaves must be in the range:

- (1) 80 – 150 MHz (2*) 8 – 25 MHz (3) 1 – 3 MHz (4) 150 – 500 kHz

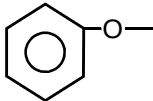
30. In an experiment for determining the gravitational acceleration g of a place with the help of a simple pendulum, the measured time period square is plotted against the string length of the pendulum in the figure.

What is the value of g at the place?

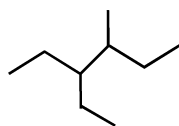


- (1) 9.81 m/s² (2*) 9.87 m/s² (3) 9.91 m/s² (4) 10.0 m/s²

PART-B-CHEMISTRY

31. Sulphur dioxide and oxygen were allowed to diffuse through a porous partition. 20 dm^3 of SO_2 diffuses through the porous partition in 60 seconds. The volume of O_2 in dm^3 which diffuses under the similar condition in 30 seconds will be (atomic mass of sulphur = 32 u):
 (1*) 14.1 (2) 10.0 (3) 7.09 (4) 28.2
32. Consider the reaction: $\text{H}_2\text{SO}_{3(\text{aq})} + \text{Sn}_{(\text{aq})}^{4+} + \text{H}_2\text{O}_{(\text{l})} \rightarrow \text{Sn}_{(\text{aq})}^{2+} + \text{HSO}_{4(\text{aq})}^{-} + 3\text{H}_{(\text{aq})}^{+}$
 Which of the following statements is correct?
 (1) Sn^{4+} is the reducing agent because it undergoes oxidation
 (2) H_2SO_3 is the reducing agent because it undergoes reducing
 (3) Sn^{4+} is the oxidizing agent because it undergoes oxidation
 (4*) H_2SO_3 is the reducing agent because it undergoes oxidation
33. Which one of the following is an example of thermosetting polymers?
 (1) Buna-N (2*) Bakelite (3) Neoprene (4) Nylon 6, 6
34. Example of a three-dimensional silicate is:
 (1) Feldspars (3) Ultramarines (3*) Beryls (4) Zeolites
35. Which one of the following ores is known as Malachite:
 (1) Cu_2O (2) CuFeS_2 (3*) $\text{Cu}(\text{OH})_2 \cdot \text{CuCO}_3$ (4) Cu_2S
36. Choose the correct statement with respect to the vapour pressure of a liquid among the following:
 (1) Increases linearly with increasing temperature
 (2) Decreases non-linearly with increasing temperature
 (3*) Increases non-linearly with increasing temperature
 (4) Decreases linearly with increasing temperature
37. Which one of the following substituents at para-position is most effective in stabilizing the phenoxide
 , ion?
 (1) $-\text{OCH}_3$ (2) CH_2OH (3*) $-\text{COCH}_3$ (4) $-\text{CH}_3$
38. Which one of the following has largest ionic radius?
 (1) Li^{+} (2) B^{3+} (3*) O_2^{2-} (4) F^{-}

39. The correct IUPAC name of the following compound:



- (1) 4-methyl-3-ethylhexane (2) 4-ethyl-3-methylhexane
(3) 3, 4-ethylmethylhexane (4*) 3-ethyl-4-methylhexane

40. Among the following organic acids, the acid present in rancid butter is:

- (1) Lactic acid (2) Pyruvic acid (3) Acetic acid (4*) Butyric acid

41. Ionization energy of gaseous Na atoms is $495.5 \text{ kJ mol}^{-1}$. The lowest possible frequency of light that ionizes a sodium atom is ($h = 6.626 \times 10^{-34} \text{ Js}$, $N_A = 6.022 \times 10^{23} \text{ mol}^{-1}$)

- (1) $7.50 \times 10^4 \text{ s}^{-1}$ (2*) $1.24 \times 10^{15} \text{ s}^{-1}$ (3) $4.76 \times 10^{14} \text{ s}^{-1}$ (4) $3.15 \times 10^{15} \text{ s}^{-1}$

42. Amongst LiCl, RbCl, BeCl₂ and MgCl₂ the compounds with the greatest and the least ionic character, respectively are:

- (1) MgCl₂ and BeCl₂ (2) LiCl and RbCl (3) RbCl and MgCl₂ (4*) RbCl and BeCl₂

43. Amongst the following identify the species with an atom in +6 oxidation state:

- (1) $[\text{Cr}(\text{CN})_6]^{3-}$ (2) Cr₂O₃ (3) $[\text{MnO}_4]^-$ (4*) CrO₂Cl₂

44. The observed osmotic pressure for a 0.10 M solution of Fe(NH₄)₂(SO₄)₂ at 25°C is 10.8 atm. The expected and experimental (observed) values of Van't Hoff factor (i) will be respectively:

($R = 0.082 \text{ L atm K}^{-1} \text{ mol}^{-1}$)

- (1) 4 and 4.00 (2) 3 and 5.42 (3*) 5 and 4.42 (4) 5 and 3.42

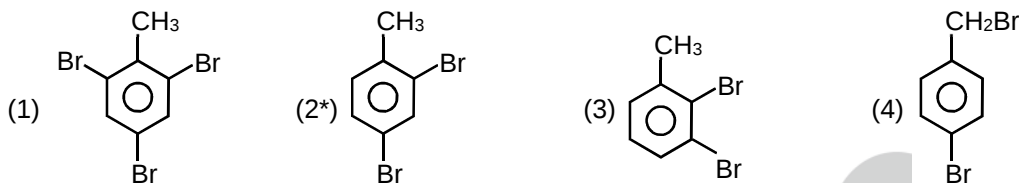
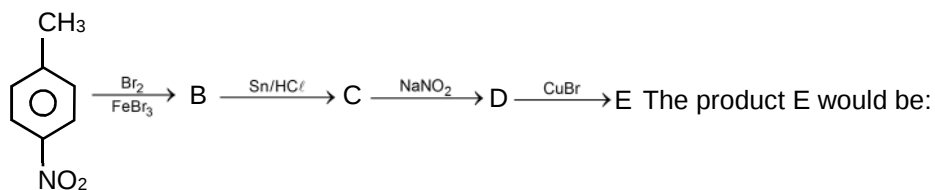
45. The reason for double helical structure of DNA is the operation of:

- (1*) Hydrogen bonding (2) Electrostatic attractions
(3) Dipole-Dipole interactions (4) van der Waals forces

46. For an ideal solution of two components A and B, which of the following is true ?

- (1) A-B interaction is stronger than A-A and B-B interactions
(2) $\Delta H_{\text{mixing}} > 0$ (zero)
(3) $\Delta H_{\text{mixing}} < 0$ (zero)
(4*) A-A, B-B and A-B interactions are identical

47. In a set of reactions p-nitrotoluene yielded a product E



48. The major product formed when 1,1,1-trichloro-propane is treated with aqueous potassium hydroxide is:
 (1) 2-Propanol (2) 1-Propanol (3) Propyne (4*) Propionic acid

49. Nickel ($Z = 28$) combines with a uninegative monodentate ligand to form a diamagnetic complex $[\text{NiL}_4]^{2-}$. The hybridisation involved and the number of unpaired electrons present in the complex are respectively:
 (1*) dsp^2 , zero (2) sp^3 , zero (3) dsp^2 , one (4) sp^3 , two

50. The final product formed when Methyl amine is treated with NaNO_2 and HCl is:
 (1) Diazomethane (2) Methylalcohol (3) Nitromethane (4) Methylcyanide

51. Which one of the following molecules is paramagnetic?
 (1) CO (2) N_2 (3) O_3 (4) NO

52. For the decomposition of the compound, represented as $\text{NH}_2\text{COONH}_4(\text{s}) \rightleftharpoons 2\text{NH}_3(\text{g}) + \text{CO}_2(\text{g})$ the $K_p = 2.9 \times 10^{-5} \text{ atm}^3$. If the reaction is started with 1 mol of the compound, the total pressure at equilibrium would be:



53. The total number of octahedral void(s) per atom present in a cubic close packed structure is:
 (1) 2 (2) 3 (3) 1 (4) 4

54. For the reaction, $3\text{A} + 2\text{B} \rightarrow \text{C} + \text{D}$,
 the differential rate law can be written as:



55. Williamson synthesis of ether is an example of:
- (1) Electrophilic addition (2) Electrophilic substitution
(3) Nucleophilic addition (4) Nucleophilic substitution
56. An octahedral complex with molecular composition $M.5NH_3.Cl.SO_4$ has two isomers, A and B. The solution of A gives a white precipitate with $AgNO_3$ solution and the solution of B gives white precipitate with $BaCl_2$ solution. the type of isomerism exhibited by the complex is:
- (1) Linkage isomerism (2*) Ionisation isomerism
(3) Coordinate isomerism (4) Geometrical isomerism
57. Zirconium phosphate $[Zr_3(PO_4)_4]$ dissociates into three zirconium cations of charge +4 and four phosphate anions of charge -3. If molar solubility of zirconium phosphate is denoted by S and its solubility product by K_{sp} then which of the following relationship between S and K_{sp} is correct?
- (1) $S = \{K_{sp} / 6912\}^{1/7}$ (2) $S = \{K_{sp} / (6912)^{1/7}\}$ (3) $S = \{K_{sp} / 144\}^{1/7}$ (4*) $S = K_{sp} / 6912^{1/7}$
58. How many electrons are involved in the following redox reaction?
- $$Cr_2O_7^{2-} + Fe^{2+} + C_2O_4^{2-} \rightarrow Cr^{3+} + Fe^{3+} + CO_2 \text{ (Unbalanced)}$$
- (1) 5 (2) 4 (3) 3 (4) 6
59. Which of these statements is not true?
- (1*) B is always covalent in its compounds
(2) $LiAlH_4$ is versatile reducing agent in organic synthesis.
(3) In aqueous solution, the Ti^{+} ion is much more stable than $Ti(III)$
(4) NO^{+} is not isoelectronic with O_2
60. Which one of the following compounds will not be soluble in sodium bicarbonate?
- (1*) o-Nitrophenol (2) 2, 4, 6-Trinitrophenol
(3) Benzene sulphonic acid (4) Benzoic acid

PART-C-MATHEMATICS

61. Equation of the line of the shortest distance between the lines $\frac{x}{1} = \frac{y}{-1} = \frac{z}{1}$ and $\frac{x-1}{0} = \frac{y+1}{-2} = \frac{z}{1}$, is
- (1) $\frac{x}{1} = \frac{y}{-1} = \frac{z}{-2}$ (2) $\frac{x-1}{1} = \frac{y+1}{-1} = \frac{z}{1}$ (3) $\frac{x}{-2} = \frac{y}{1} = \frac{z}{2}$ (4*) $\frac{x-1}{1} = \frac{y+1}{-1} = \frac{z}{-2}$
62. Let $\bar{x}$, M and σ^2 be respectively the mean, mode and variance of n observations $x_1, x_2, \dots, x_n$ and $d_i = -x_i - a$, $i = 1, 2, \dots, n$ where a is any number.
- Statement-I: Variance of $d_1, d_2, \dots, d_n$ is σ^2 .
- Statement-II: Mean and mode of $d_1, d_2, \dots, d_n$ are $-\bar{x} - a$ and $-M - a$, respectively.
- (1) Statement-I is true and statement-II is false.
 (2*) Statement-I and statement-II are both true.
 (3) Statement-I is false and statement-II is true.
 (4) Statement-I and statement-II are both false.
63. The function $f(x) = |\sin 4x| + |\cos 2x|$, is a periodic function with period
- (1) π (2) $\frac{\pi}{4}$ (3*) $\frac{\pi}{2}$ (4) 2π
64. Let function F be defined as $F(x) = \int_1^x \frac{e^t}{t} dt$, $x > 0$ then the value of the integral $\int_1^x \frac{e^t}{t+a} dt$, where $a > 0$, is
- (1) $e^a[F(x) - F(1+a)]$ (2*) $e^{-a}[F(x+a) - F(1+a)]$
 (3) $e^{-a}[F(x+a) - F(a)]$ (4) $e^a[F(x+a) - F(1+a)]$
65. A chord is drawn through the focus of the parabola $y^2 = 6x$ such that its distance from the vertex of this parabola is $\frac{\sqrt{5}}{2}$, then its slope can be
- (1*) $\frac{\sqrt{5}}{2}$ (2) $\frac{\sqrt{3}}{2}$ (3) $\frac{2}{\sqrt{5}}$ (4) $\frac{2}{\sqrt{3}}$
66. The principal value of $\tan^{-1}\left(\cot \frac{43\pi}{4}\right)$, is
- (1) $\frac{3\pi}{4}$ (2) $\frac{-3\pi}{4}$ (3*) $\frac{-\pi}{4}$ (4) $\frac{\pi}{4}$
67. The equation of the circle described on the chord $3x + y + 5 = 0$ of the circle $x^2 + y^2 = 16$ as diameter is
- (1) $x^2 + y^2 + 3x + y + 1 = 0$ (2*) $x^2 + y^2 + 3x + y - 11 = 0$
 (3) $x^2 + y^2 + 3x + y - 22 = 0$ (4) $x^2 + y^2 + 3x + y - 2 = 0$

68. Two women and some men participated in a chess tournament in which every participant played two games with each of the other participants. If the number of games that the men played between themselves exceeds the number of games that the men played with the women by 66, then the number of men who participated in the tournament lies in the interval
 (1*) [10, 12] (2) (14, 17) (3) [8, 9] (4) (11, 13]
69. If the volume of a spherical ball is increasing at the rate of 4π cc/sec, then the rate of increase of its radius (in cm/sec), when the volume is 288π cc, is
 (1*) $\frac{1}{36}$ (2) $\frac{1}{24}$ (3) $\frac{1}{24}$ (4) $\frac{1}{9}$
70. Let $f(n) = \left[\frac{1}{3} + \frac{3n}{100} \right] n$, where $[n]$ denotes the greatest integer less than or equal to n . Then $\sum_{n=1}^{56} f(n)$ is equal to
 (1*) 1399 (2) 1287 (3) 56 (4) 689
71. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = \frac{|x|-1}{|x|+1}$ then f is
 (1) both one-one and onto (2*) neither one-one nor onto
 (3) onto but not one-one (4) one-one but not onto
72. If $\frac{dy}{dx} + y \tan x = \sin 2x$ and $y(0) = 1$, then $y(\pi)$ is equal to
 (1) -1 (2) 5 (3) 1 (4*) -5
73. If m is a non-zero number and $\int \frac{x^{5m-1} + 2x^{4m-1}}{(x^{2m} + x^m + 1)^3} dx = f(x) + C$, then $f(x)$ is
 (1) $\frac{(x^{5m} - x^{4m})}{2m(x^{2m} + x^m + 1)^2}$ (2*) $\frac{x^{4m}}{2m(x^{2m} + x^m + 1)^2}$ (3) $\frac{2m(x^{5m} + x^{4m})}{(x^{2m} + x^m + 1)^2}$ (4) $\frac{x^{5m}}{2m(x^{2m} + x^m + 1)^2}$
74. If the angle between the line $2(x+1) = y = z+4$ and the plane $2x - y + \sqrt{\lambda}z + 4 = 0$ is $\frac{\pi}{6}$, then the value of λ is
 (1) $\frac{135}{7}$ (2) $\frac{45}{11}$ (3*) $\frac{45}{7}$ (4) $\frac{135}{11}$

75. If $\Delta_r = \begin{vmatrix} r & 2r-1 & 3r-2 \\ \frac{n}{2} & n-1 & a \\ \frac{1}{2}n(n-1) & (n-1)^2 & \frac{1}{2}(n-1)(3n+4) \end{vmatrix}$ then the value of $\sum_{r=1}^{n-1} \Delta_r$
- (1*) is independent of both a and n. (2) depends only on a.
 (3) depends both on a and n. (4) depends only on n.
76. The circumcentre of a triangle lies at the origin and its centroid is the mid point of the line segment joining the points $(a^2 + 1, a^2 + 1)$ and $(2a, -2a)$, $a \neq 0$. Then for any a, the orthocentre of this triangle lies on the line
- (1) $y - 2ax = 0$ (2) $y + x = 0$
 (3*) $(a - 1)^2x - (a + 1)^2y = 0$ (4) $y - (a^2 + 1)x = 0$
77. The coefficient of x^{1012} in the expansion of $(1 + x^n + x^{253})^{10}$, (where $n \leq 22$ is any positive integer), is
- (1) $^{253}C_4$ (2) $4n$ (3) 1 (4*) $^{10}C_4$
78. If non-zero real numbers b and c are such that $\min. f(x) > \max. g(x)$ where $f(x) = x^2 + 2bx + 2c^2$ and $g(x) = -x^2 - 2cx + b^2$ ($x \in \mathbb{R}$), then $\left| \frac{c}{b} \right|$ lies in the interval
- (1) $\left[\frac{1}{\sqrt{2}}, \sqrt{2} \right]$ (2*) $(\sqrt{2}, \infty)$ (3) $\left(0, \frac{1}{2} \right)$ (4) $\left[\frac{1}{2}, \frac{1}{\sqrt{2}} \right]$
79. Let A and E be any two events with positive probabilities:
 Statement-1: $P(E/A) \geq P(A/E) P(E)$
 Statement-2: $P(A/E) \geq P(A \cap E)$
- (1) Both the statements are false. (2*) Both the statements are true.
 (3) Statement-1 is false, statement-2 is true. (4) Statement-1 is true, statement-2 is false.
80. If a line L is perpendicular to the line $5x - y = 1$, and the area of the triangle formed by the line L and the coordinate axes is 5, then the distance of line L from the line $x + 5y = 0$ is
- (1) $\frac{7}{\sqrt{5}}$ (2) $\frac{5}{\sqrt{7}}$ (3*) $\frac{5}{\sqrt{13}}$ (4) $\frac{7}{\sqrt{13}}$
81. If the function $f(x) = \begin{cases} \frac{\sqrt{2 + \cos x} - 1}{(\pi - x)^2}, & x \neq \pi \\ k, & x = \pi \end{cases}$ is continuous at $x = \pi$, then k equals
- (1) $\frac{1}{2}$ (2*) $\frac{1}{4}$ (3) 0 (4) 2

82. For all complex numbers z of the form $1 + i\alpha$, $\alpha \in \mathbb{R}$, if $z^2 = x + iy$, then
 (1) $y^2 + 4x + 2 = 0$ (2) $y^2 - 4x + 4 = 0$ (3*) $y^2 + 4x - 4 = 0$ (4) $y^2 - 4x + 2 = 0$
83. The tangent at an extremity (in the first quadrant) of latus rectum of the hyperbola $\frac{x^2}{4} - \frac{y^2}{5} = 1$, meets x -axis and y -axis at A and B respectively. Then $(OA)^2 - (OB)^2$, where O is the origin equals
 (1) $-\frac{4}{3}$ (2) $\frac{16}{9}$ (3) 4 (4*) $-\frac{20}{9}$
84. If $\vec{x} = 3\hat{i} - 6\hat{j} - \hat{k}$, $\vec{y} = \hat{i} + 4\hat{j} - 3\hat{k}$ and $\vec{z} = 3\hat{i} - 4\hat{j} - 12\hat{k}$, then the magnitude of the projection of $\vec{x} \times \vec{y}$ on $\vec{z}$ is
 (1) 13 (2*) 14 (3) 15 (4) 12
85. The area of the region above the x -axis bounded by the curve $y = \tan x$, $0 \leq x \leq \frac{\pi}{2}$ and the tangent to the curve at $x = \frac{\pi}{4}$ is
 (1) $\frac{1}{2}(1 - \log 2)$ (2) $\frac{1}{2}\left(\log 2 + \frac{1}{2}\right)$ (3) $\frac{1}{2}(1 + \log 2)$ (4*) $\frac{1}{2}\left(\log 2 - \frac{1}{2}\right)$
86. The equation $\sqrt{3x^2 + x + 5} = x - 3$, where x is real, has
 (1) exactly two solutions (2) exactly four solutions
 (3) exactly one solution (4*) no solution
87. Let A and B be any two 3×3 matrices. If A is symmetric and B is skewsymmetric, then the matrix $AB - BA$ is
 (1) neither symmetric nor skewsymmetric. (2*) symmetric
 (3) I or $-I$, where I is an identity matrix (4) skewsymmetric
88. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a function such that $|f(x)| \leq x^2$, for all $x \in \mathbb{R}$. Then, at $x = 0$, f is
 (1) continuous but not differentiable. (2) differentiable but not continuous.
 (3*) continuous as well as differentiable. (4) neither continuous nor differentiable.
89. The number of terms in an A.P. is even; the sum of the odd terms in it is 24 and that the even terms is 30. If the last term exceeds the first term by $10\frac{1}{2}$, then the number of terms in the A.P. is
 (1) 4 (2) 16 (3*) 8 (4) 12
90. The contrapositive of the statement "if I am not feeling well, then I will go to the doctor" is
 (1) If I will go to the doctor, then I am not feeling well.
 (2) If I am feeling well, then I will not go to the doctor.
 (3*) If I will not go to the doctor, then I am feeling well.
 (4) If I will go to the doctor, then I am feeling well.