

**JEE (MAIN)-2015****ONLINE_11-04-2015****IMPORTANT INSTRUCTIONS**

1. The test is of **3** hours duration.
2. The Test Booklet consists of **90** questions. The maximum marks are **360**.
3. There are **three** parts in the question paper A, B, C consisting of **Physics, Chemistry and Mathematics** having 30 questions in each part of equal weightage. Each question is allotted **4 (four)** marks for each correct response.
4. Candidates will be awarded marks as stated above in instruction No.3 for correct response of each question. 1/4 (one fourth) marks will be deducted for indicating incorrect response of each question. No deduction from the total score will be made if no response is indicated for an item in the answer sheet.
5. There is only one correct response for each question. Filling up more than one response in each question will be treated as wrong response and marks for wrong response will be deducted accordingly as per instruction 4 above.

PART-A-PHYSICS

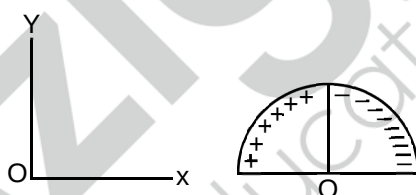
1. A particle is moving in a circle of radius r under the action of a force $F = \alpha r^2$ which is directed towards centre of the circle. Total mechanical energy (kinetic energy + potential energy) of the particle is (take potential energy = 0 for $r = 0$) :

(1) $\frac{4}{3} \alpha r^3$ (2) $\frac{5}{6} \alpha r^3$ (3) αr^3 (4) $\frac{1}{2} \alpha r^3$

2. A beaker contains a fluid of density ρ kg/m³, specific heat S J/kg°C and viscosity η . The beaker is filled up to height h . To estimate the rate of heat transfer per unit area (Q/A) by convection when beaker is put on a hot plate, a student proposes that it should depend on η , $\left(\frac{S\Delta\theta}{h}\right)$ and $\left(\frac{1}{\rho g}\right)$ when $\Delta\theta$ (in °C) is difference in the temperature between the bottom and top of the fluid. In that situation the correct option for (Q/A) is :

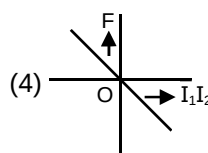
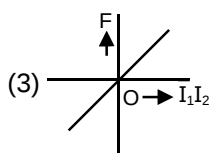
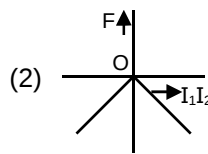
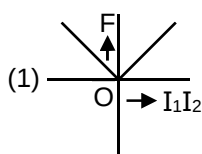
(1) $\eta \left(\frac{S\Delta\theta}{h}\right) \left(\frac{1}{\rho g}\right)$ (2) $\eta \frac{S\Delta\theta}{h}$ (3) $\left(\frac{S\Delta\theta}{\eta h}\right) \left(\frac{1}{\rho g}\right)$ (4) $\frac{S\Delta\theta}{\eta h}$

3. A wire of length L ($= 20$ cm) is bent into a semi-circular arc. If the two equal halves of the arc, were each to be uniformly charged with charges $\pm Q$, [$Q = 10^3 \epsilon_0$ Coulomb where ϵ_0 is the permittivity (in SI unit) of free space] the net electric field at the centre O of the semi-circular arc would be :

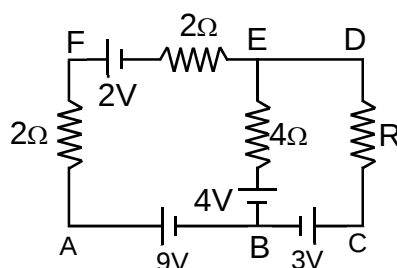


(1) $(50 \times 10^3 \text{ N/C}) \hat{j}$ (2) $(25 \times 10^3 \text{ N/C}) \hat{j}$ (3) $(50 \times 10^3 \text{ N/C}) \hat{j}$ (4*) $(25 \times 10^3 \text{ N/C}) \hat{j}$

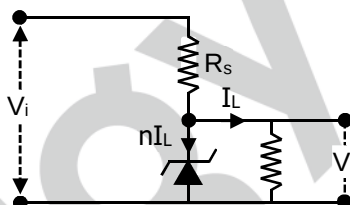
4. Two long straight parallel wires carrying (adjustable) currents I_1 and I_2 , are kept at a distance d apart. If the force ' F ' between the two wires is taken as 'positive' when the wires repel each other and 'negative' when the wires attract each other, the graph showing the dependence of ' F ', on the product $I_1 I_2$, would be :



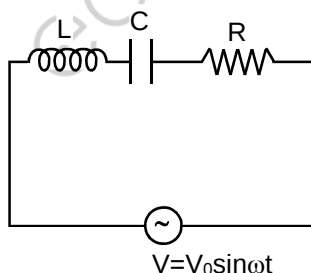
5. In the electric network shown, when no current flows through the 4Ω resistor in the arm EB, the potential difference between the points A and D will be :



- (1) 5 V (2) 6 V (3) 4 V (4) 3 V
6. Using equipartition of energy, the specific heat (in $\text{J kg}^{-1}\text{K}^{-1}$) of aluminium at room temperature can be estimated to be (atomic weight of aluminium = 27)
- (1) 925 (2) 1850 (3*) 25 (4) 410
7. The value of the resistor R_s , needed in the dc voltage regulator circuit shown here, equals :



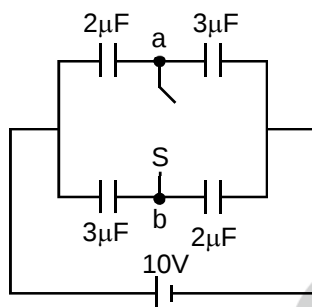
- (1) $(V_i - V_L)/(n + 1)I_L$ (2) $(V_i + V_L)/nI_L$ (3) $(V_i + V_L)/(n + 1)I_L$ (4) $(V_i - V_L)/nI_L$
8. For the LCR circuit, shown here, the current is observed to lead the applied voltage. An additional capacitor C' , when joined with the capacitor C present in the circuit, makes the power factor of the circuit unity. The capacitor C' , must have been connected in :



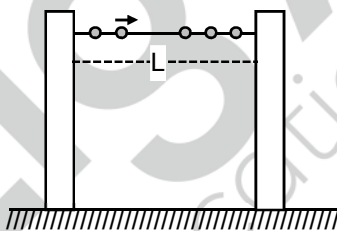
- (1) series with C and has a magnitude $\frac{1 - \omega^2 LC}{\omega^2 L}$
- (2) series with C and has a magnitude $\frac{C}{\omega^2 LC - 1}$
- (3) parallel with C has a magnitude $\frac{1 - \omega^2 LC}{\omega^2 L}$
- (4) parallel with C and has a magnitude $\frac{C}{(\omega^2 LC - 1)}$

9. An electric field $\vec{E} = (25\hat{i} + 30\hat{j})\text{NC}^{-1}$ exists in a region of space. If the potential at the origin is taken to be zero then the potential at $x = 2, y = 2$ m is :
- (1) -120 J (2) -130 J (3) -110 J (4) -140 J

10. In figure is shown a system of four capacitors connected across a 10 V battery. Charge that will flow from switch S when it is closed is :

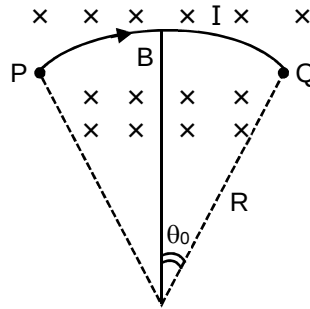


- (1) $5\text{ }\mu\text{C}$ from a to b (2) zero (3) $5\text{ }\mu\text{C}$ from b to a (4) $20\text{ }\mu\text{C}$ from a to b
11. A large number (n) of identical beads, each of mass m and radius r are strung on a thin smooth rigid horizontal rod of length L ($L \gg r$) and are at rest at random positions. The rod is mounted between two rigid supports (see figure). If one of the beads is now given a speed v , the average force experienced by each support after a long time is (assume all collisions are elastic) :

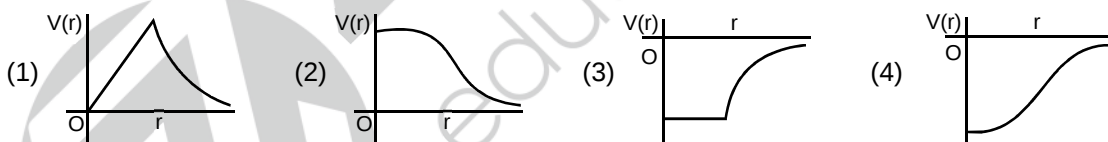


- (1) $\frac{mv^2}{L - nr}$ (2) $\frac{mv^2}{2(L - nr)}$ (3) $\frac{mv^2}{L - 2nr}$ (4) zero
12. A particle of mass 2 kg is on a smooth horizontal table and moves in a circular path of radius 0.6 m. The height of the table from the ground is 0.8 m. If the angular speed of the particle is 12 rad s^{-1} , the magnitude of its angular momentum about a point on the ground right under the centre of the circle is :
- (1) $20.16\text{ kg m}^2\text{s}^{-1}$ (2) $11.52\text{ kg m}^2\text{s}^{-1}$ (3) $8.64\text{ kg m}^2\text{s}^{-1}$ (4) $14.4\text{ kg m}^2\text{s}^{-1}$
13. A cylindrical block of wood (density $= 650\text{ kg m}^{-3}$), of base area 30 cm^2 and height 54 cm , floats in a liquid of density 900 kg m^{-3} . The block is depressed slightly and then released. The time period of the resulting oscillation of the block would be equal to that of a simple pendulum of length (nearly) :
- (1) 39 cm (2) 65 cm (3) 26 cm (4) 52 cm
14. The de-Broglie wavelength associated with the electron in the $n = 4$ level is :
- (1) two times the de-Broglie wavelength of the electron in the ground state
 (2) half of the de-Broglie wavelength of the electron in the ground state
 (3) four times the de-Broglie wavelength of the electron in the ground state
 (4) $1/4^{\text{th}}$ of the de-Broglie wavelength of the electron in the ground state

15. A wire carrying current I is tied between points P and Q and is in the shape of a circular arch of radius R due to a uniform magnetic field B (perpendicular to the plane of the paper, shown by $\times$) in the vicinity of the wire. If the wire subtends an angle $2\theta_0$ at the centre of the circle (of which it forms an arch) then the tension in the wire is :



- (1) IBR (2) $\frac{IBR\theta_0}{\sin\theta_0}$ (3) $\frac{IBR}{\sin\theta_0}$ (4) $\frac{IBR}{2\sin\theta_0}$
16. Unpolarized light of intensity I_0 is incident on surface of a block of glass at Brewster's angle. In that case, which one of the following statement is true ?
- (1) reflected light is partially polarized with intensity $I_0/2$
 (2) reflected light is completely polarized with intensity less than $I_0/2$.
 (3) transmitted light is partially polarized with intensity $I_0/2$
 (4) transmitted light is completely polarized with intensity less than $I_0/2$
17. Which of the following most closely depicts the correct variation of the gravitation potential $V(r)$ due to a large planet of radius R and uniform mass density ? (figures are not drawn to scale)



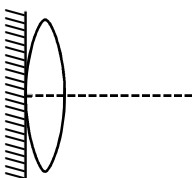
18. A short bar magnet is placed in the magnetic meridian of the earth with north pole pointing north. Neutral points are found at a distance of 30 cm from the magnet on the East - West line, drawn through the middle point of the magnet. The magnetic moment of the magnet in Am^2 is close to :

(Given $\frac{\mu_0}{4\pi} = 10^{-7}$ in SI units and

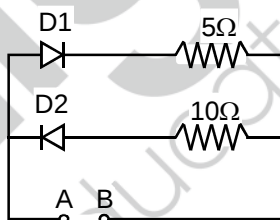
B_H = Horizontal component of earth's magnetic field = 3.6×10^{-5} Tesla)

- (1) 4.9 (2) 14.6 (3) 9.7 (4) 19.4
19. The AC voltage across a resistance can be measured using a :
- (1) hot wire voltmeter (2) moving magnet galvanometer
 (3) moving coil galvanometer (4) potentiometer

20. A thin convex lens of focal length 'f' is put on a plane mirror as shown in the figure. When an object is kept at a distance 'a' from the lens - mirror combination, its image is formed at a distance $\frac{a}{3}$ in front of the combination. The value of 'a' is :



- (1) $2f$ (2) $\frac{3}{2}f$ (3) $3f$ (4) f
21. In a Young's double slit experiment with light of wavelength λ the separation of slits is d and distance of screen is D such that $D \gg d \gg \lambda$. If the Fringe width is β , the distance from point of maximum intensity to the point where intensity falls to half of maximum intensity on either side is :
- (1) $\frac{\beta}{2}$ (2) $\frac{\beta}{6}$ (3) $\frac{\beta}{4}$ (4) $\frac{\beta}{3}$
22. A 2V battery is connected across AB as shown in the figure. The value of the current supplied by the battery when in one case battery's positive terminal is connected to A and in other case when positive terminal of battery is connected to B will respectively be :



- (1) 0.4 A and 0.2 A (2) 0.2 A and 0.1 A (3) 0.1 A and 0.2 A (4) 0.2 A and 0.4 A
23. A uniform thin rod AB of length L has linear mass density $\mu(x) = a + \frac{bx}{L}$, where x is measured from A. If the CM of the rod lies at a distance of $\left(\frac{7}{12}L\right)$ from A, then a and b are related as :
- (1) $3a = 2b$ (2) $a = b$ (3) $2a = b$ (4) $a = 2b$
24. A vector $\vec{A}$ is rotated by a small angle $\Delta\theta$ radians ($\Delta\theta \ll 1$) to get a new vector $\vec{B}$. In that case $|\vec{B} - \vec{A}|$ is :
- (1) $|\vec{A}| \Delta\theta$ (2) $|\vec{A}| \left(1 - \frac{\Delta\theta^2}{2}\right)$ (3) 0 (4) $|\vec{B}| \Delta\theta - |\vec{A}|$

25. If electronic charge e , electron mass m , speed of light in vacuum c and Planck's constant h are taken as fundamental quantities, the permeability of vacuum μ_0 can be expressed in units of :

(1) $\left(\frac{h}{ce^2}\right)$ (2) $\left(\frac{mc^2}{he^2}\right)$ (3) $\left(\frac{h}{me^2}\right)$ (4) $\left(\frac{hc}{me^2}\right)$

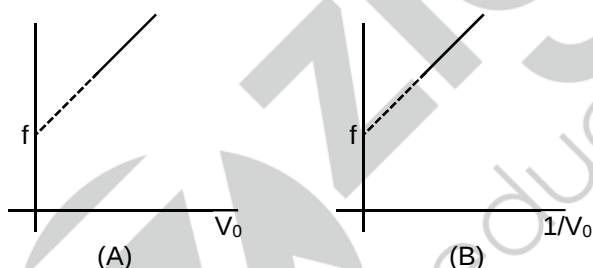
26. Let N_β be the number of β particles emitted by 1 gram of Na^{24} radioactive nuclei (half life = 15 hrs) in 7.5 hours, N_β is close to (Avogadro number = 6.023×10^{23} /g. mole)

(1) 7.5×10^{21} (2) 6.2×10^{21} (3) 1.25×10^{22} (4) 1.75×10^{22}

27. An experiment takes 10 minutes to raise the temperature of water in a container from 0°C to 100°C and another 55 minutes to convert it totally into steam by a heater supplying heat at a uniform rate. Neglecting the specific heat of the container and taking specific heat of water to be $1 \text{ cal/g } ^\circ\text{C}$, the heat of vaporization according to this experiment will come out to be :

(1) 550 cal/g (2*) 560 cal/g (3) 540 cal/g (4) 530 cal/g

28. A source of sound emits sound waves at frequency f_0 . It is moving towards an observer with fixed speed v_s ($v_s < v$, where v is the speed of sound in air). If the observer were to move towards the source with speed v_0 , one of the following two graphs (A and B) will give the correct variation of the frequency f heard by the observer as v_0 is changed. The variation of f with v_0 is given correctly by :



(1) graph A with slope = $\frac{f_0}{(v + v_s)}$ (2) graph B with slope = $\frac{f_0}{(v + v_s)}$
 (3) graph A with slope = $\frac{f_0}{(v - v_s)}$ (4) graph B with slope = $\frac{f_0}{(v - v_s)}$

29. A pendulum with time period of 1s is losing energy due to damping. At certain time its energy is 45J. If after completing 15 oscillations, its energy has become 15J, its damping constant (in s^{-1}) is :

(1) $\frac{1}{2}$ (2) 2 (3) $\frac{1}{15} \ln 3$ (4) $\frac{1}{30} \ln 3$

30. For plane electromagnetic waves propagating in the z direction, which one of the following combination gives the correct possible direction for $\vec{E}$ and $\vec{B}$ field respectively ?

(1) $(3\hat{i} + 4\hat{j})$ and $(4\hat{i} - 3\hat{j})$ (2) $(-2\hat{i} - 3\hat{j})$ and $(3\hat{i} - 2\hat{j})$
 (3) $(\hat{i} + 2\hat{j})$ and $(2\hat{i} - \hat{j})$ (4) $(2\hat{i} + 3\hat{j})$ and $(\hat{i} + 2\hat{j})$

PART-B-CHEMISTRY

31. Chlorine water on standing loses its colour and forms :
 (1) HCl and HOCl (2) HCl only (3) HOCl and HOCl₂ (4) HCl and HClO₂
32. The increase of pressure on ice $\rightleftharpoons$ water system at constant temperature will lead to :
 (1) a shift of the equilibrium in the forward direction
 (2) an increase in the Gibbs energy of the system
 (3) a decrease in the entropy of the system
 (4) no effect on the equilibrium
33. Which of the alkaline earth metal halides given below is essentially covalent in nature ?
 (1) CaCl₂ (2) BeCl₂ (3) SrCl₂ (4) MgCl₂
34. Addition of phosphate fertilisers to water bodies causes :
 (1) enhanced growth of algae (2) increase in amount of dissolved oxygen in water
 (3) increase in fish population (4) deposition of calcium phosphate
35. Which of the following compounds has a P–P bond ?
 (1) H₄P₂O₇ (2) H₄P₂O₇ (3) (HPO₃)₃ (4) H₄P₂O₆
36. Accumulation of which of the following molecules in the muscles occurs as a result of vigorous exercise ?
 (1) Glycogen (2) L-lactic acid (3) Pyruvic acid (4) Glucose
37. In the reaction sequence
 $2 \text{CH}_3\text{CHO} \xrightarrow{\text{OH}^-} \text{A} \xrightarrow{\Delta} \text{B}$; the product B is :
 (1) CH₃–CH₂–CH₂–CH₂–OH (2) CH₃–CH=CH–CHO
 (3) CH₃– $\overset{\text{O}}{\parallel}$ –CH₃ (4) CH₃–CH₂–CH₂–CH₃
38. For the equilibrium, A(g) $\rightleftharpoons$ B(g), ΔH is – 40kJ/mol. If the ratio of the activation energies of the forward (E_f) and reverse (E_b) reactions is $\frac{2}{3}$ then :
 (1) E_f = 30 kJ/mol ; E_b = 70 kJ/mol
 (2) E_f = 80 kJ/mol ; E_b = 120 kJ/mol
 (3) E_f = 60 kJ/mol ; E_b = 100 kJ/mol
 (4) E_f = 70 kJ/mol ; E_b = 30 kJ/mol

39. Match the organic compounds in column-I with the Lassaigne's test results in column-II appropriately :

Column- I

- (A) Aniline
 (B) Benzene sulfonic acid
 (C) Thiourea
 (1) (A)–(iii), (B)–(ii), (C)–(i)
 (3) (A)–(iii), (B)–(i), (C)–(ii)

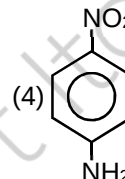
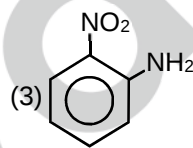
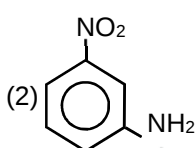
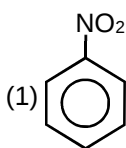
Column- II

- (i) Red color with FeCl_3
 (ii) Violet color with sodium nitroprusside
 (iii) Blue color with hot and acidic solution of FeSO_4
 (2) (A)–(ii), (B)–(i), (C)–(iii)
 (4) (A)–(ii), (B)–(iii), (C)–(i)

40. Which of the following complex ions has electrons that are symmetrically filled in both t_{2g} and e_g orbitals?

- (1) $[\text{FeF}_6]^{3-}$ (2) $[\text{Mn}(\text{CN})_6]^{4-}$ (3) $[\text{Co}(\text{NH}_3)_6]^{2+}$ (4) $[\text{CoF}_6]^{3-}$

41. Which compound exhibits maximum dipole moment among the following ?



42. Which physical property of dihydrogen is wrong ?

- (1) Tasteless gas (2) Non-inflammable gas
 (3) Odourless gas (4) Colourless gas

43. A pink coloured salt turns blue on heating. The presence of which cation is most likely ?

- (1) Zn^{2+} (2) Fe^{2+} (3) Cu^{2+} (4) Co^{2+}

44. $\text{A} + 2\text{B} \rightarrow \text{C}$, the rate equation for this reaction is given as

$$\text{Rate} = k[\text{A}][\text{B}]$$

If the concentration of A is kept the same but that of B is doubled what will happen to the rate itself ?

- (1) halved (2) quadrupled (3) doubled (4) the same

45. Determination of the molar mass of acetic acid in benzene using freezing point depression is affected by :

- (1) partial ionization (2) dissociation (3) complex formation (4) association

46. Which artificial sweetener contains chlorine ?

- (1) Sucralose (2) Aspartame (3) Alitame (4) Saccharin

47. When concentrated HCl is added to an aqueous solution of CoCl_2 , its colour changes from reddish pink to deep blue. Which complex ion gives blue colour in this reaction ?

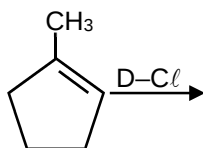
- (1) $[\text{Co}(\text{H}_2\text{O})_6]^{2+}$ (2) $[\text{CoCl}_6]^{3-}$ (3) $[\text{CoCl}_4]^{2-}$ (4) $[\text{CoCl}_6]^{4-}$

48. At temperature T , the average kinetic energy of any particle is $\frac{3}{2} kT$. The de Broglie wavelength follows the order :
- (1) Visible photon > Thermal neutron > Thermal electron
 - (2) Visible photon > Thermal electron > Thermal neutron
 - (3) Thermal proton > Thermal electron > Visible photon
 - (4) Thermal proton > Visible photon > Thermal electron
49. Which of the following statements is false ?
- (1) CrO_4^{2-} is tetrahedral in shape
 - (2) $\text{Na}_2\text{Cr}_2\text{O}_7$ is less soluble than $\text{K}_2\text{Cr}_2\text{O}_7$
 - (3) $\text{Cr}_2\text{O}_7^{2-}$ has a $\text{Cr}-\text{O}-\text{Cr}$ bond
 - (4) $\text{Na}_2\text{Cr}_2\text{O}_7$ is a primary standard in volumetry
50. When does a gas deviate the most from its ideal behaviour ?
- (1) At high pressure and low temperature
 - (2) At low pressure and low temperature
 - (3) At low pressure and high temperature
 - (4) At high pressure and high temperature
51. Which of the following pairs of compounds are positional isomers ?
- (1) $\text{CH}_3-\text{CH}_2-\text{CH}_2-\overset{\text{O}}{\underset{\text{O}}{\text{C}}}-\text{CH}_3$ and $\text{CH}_3-\underset{\text{CH}_3}{\text{CH}}-\text{CH}_2-\text{CHO}$
 - (2) $\text{CH}_3-\text{CH}_2-\text{CH}_2-\text{CH}_2-\text{CHO}$ and $\text{CH}_3-\text{CH}_2-\text{CH}_2-\overset{\text{O}}{\underset{\text{O}}{\text{C}}}-\text{CH}_3$
 - (3) $\text{CH}_3-\text{CH}_2-\overset{\text{O}}{\underset{\text{O}}{\text{C}}}-\text{CH}_2-\text{CH}_3$ and $\text{CH}_3-\text{CH}_2-\text{CH}_2-\text{CH}_3$ and $\text{CH}-\text{CH}_2-\text{CHO}$
 - (4) $\text{CH}_3-\text{CH}_2-\text{CH}_2-\overset{\text{O}}{\underset{\text{O}}{\text{C}}}-\text{CH}_3$ and $\text{CH}_3-\text{CH}_2-\overset{\text{O}}{\underset{\text{O}}{\text{C}}}-\text{CH}_2-\text{CH}_3$
52. Choose the incorrect formula out of the four compounds for an element X below :
- (1) $\text{X}_2(\text{SO}_4)_3$
 - (2) X_2O_3
 - (3) X_2Cl_3
 - (4) XPO_4
53. The number of structural isomers for C_6H_{14} is :
- (1) 3
 - (2) 4
 - (3) 6
 - (4) 5
54. At 298 K, the standard reduction potentials are 1.51 V for $\text{MnO}_4^-|\text{Mn}^{2+}$, 1.36 V for $\text{Cl}_2|\text{Cl}^-$, 1.07 V for $\text{Br}_2|\text{Br}^-$, and 0.54 V for $\text{I}_2|\text{I}^-$. At pH = 3, permanganate is expected to oxidize : $\left(\frac{RT}{F} = 0.059\text{V}\right)$
- (1) Cl^- , Br^- and I^-
 - (2) Cl^- and Br^-
 - (3) I^- only
 - (4) Br^- and I^-

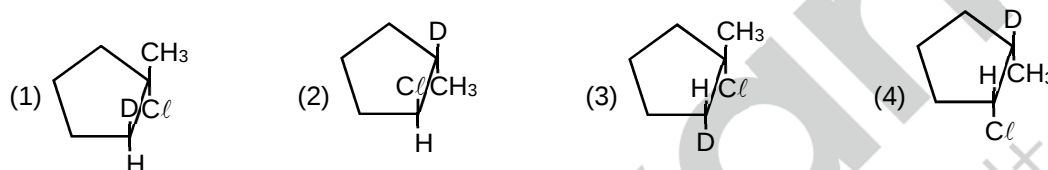
55. Under ambient conditions, which among the following surfactants will form micelles in aqueous solution at lowest molar concentration ?



56. What is the major product expected from the following reaction ?



Where D is an isotope of Hydrogen.



57. Molecule AB has a bond length of $1.617 \text{ \AA}$ and a dipole moment of 0.38 D . The fractional charge on each atom (absolute magnitude) is : ($e_0 = 4.802 \times 10^{-10} \text{ esu}$)

- (1) 1.0 (2) 0.05 (3) 0 (4) 0.5

58. $\text{A} + 2\text{B} + 3\text{C} \rightarrow \text{AB}_2\text{C}_3$

Reaction of 6.0 g of A, 6.0×10^{23} atoms of B, and 0.036 mol of C yields 4.8 g of compound AB_2C_3 . If the atomic mass of A and C are 60 and 80 amu , respectively, the atomic mass of B is

(Avogadro no. = 6×10^{23}) :

- (1) 50 amu (2) 60 amu (3) 70 amu (4) 40 amu

59. Which one of the following structures represents the neoprene polymer ?



60. Calamine is an ore of :

- (1) Iron (2) Zinc (3) Aluminium (4) Copper

PART-C-MATHEMATICS

61. The term independent of x in the binomial expansion of $\left(1 - \frac{1}{x} + 3x^5\right)\left(2x^2 - \frac{1}{x}\right)^8$ is
 (1) 496 (2) -496 (3*) 400 (4) -400
62. Let PQ be a double ordinate of the parabola, $y^2 = -4x$, where P lies in the second quadrant. If R divides PQ in the ratio 2 : 1, then the locus of R is
 (1) $9y^2 = -4x$ (2) $3y^2 = -2x$ (3) $3y^2 = 2x$ (4) $9y^2 = 4x$
63. If a circle passing through the point $(-1, 0)$ touches y -axis at $(0, 2)$, then the length of the chord of the circle along the x -axis is
 (1*) 3 (2) $\frac{3}{2}$ (3) $\frac{5}{2}$ (4) 5
64. If the two roots of the equation $(a - 1)(x^4 + x^2 + 1) + (a + 1)(x^2 + x + 1)^2 = 0$ are real and distinct, then the set of all values of 'a' is
 (1) $\left(0, \frac{1}{2}\right)$ (2*) $\left(\frac{-1}{2}, 0\right) \cup \left(0, \frac{1}{2}\right)$ (3) $\left(\frac{-1}{2}, 0\right)$ (4) $(-\infty, -2) \cup (2, \infty)$
65. In a parallelogram ABCD, $|\overline{AB}| = a, |\overline{AD}| = b$ and $|\overline{AC}| = c$, then $\overline{DB} \cdot \overline{AB}$ has the value
 (1) $\frac{1}{4}(a^2 + b^2 - c^2)$ (2) $\frac{1}{2}(a^2 + b^2 + c^2)$ (3) $\frac{1}{3}(b^2 + c^2 - a^2)$ (4) $\frac{1}{4}(a^2 - b^2 + c^2)$
66. Let $A = \{x_1, x_2, \dots, x_7\}$ and $B = \{y_1, y_2, y_3\}$ be two sets containing seven and three distinct elements respectively. Then the total number of functions $f : A \rightarrow B$ that are onto, if there exist exactly three elements x in A such that $f(x) = y_2$, is equal to
 (1*) $14 \cdot {}^7C_3$ (2) $14 \cdot {}^7C_2$ (3) $14 \cdot {}^7C_2$ (4) $16 \cdot {}^7C_3$
67. Let k be a non-zero real number. If $f(x) = \begin{cases} \frac{(e^x - 1)^2}{\sin\left(\frac{x}{k}\right) \log\left(1 + \frac{x}{4}\right)}, & x \neq 0 \\ 12, & x = 0 \end{cases}$ is a continuous function, then the value of k is
 (1*) 3 (2) 1 (3) 4 (4) 2
68. If $\sum_{n=1}^5 \frac{1}{n(n+1)(n+2)(n+3)} = \frac{k}{3}$, then k is equal to
 (1*) $\frac{55}{336}$ (2) $\frac{19}{112}$ (3) $\frac{17}{105}$ (4*) $\frac{1}{6}$

69. If z is a non-real complex number, then the minimum value of $\frac{\operatorname{Im} z^5}{(\operatorname{Im} z)^5}$ is
 (1) -4 (2) -5 (3) -1 (4) -2
70. A straight line L through the point $(3, -2)$ is inclined at an angle of 60° to the line $\sqrt{3}x + y = 1$. If L also intersects the x -axis, then the equation of L is
 (1) $\sqrt{3}y - x + 3 + 2\sqrt{3} = 0$ (2) $\sqrt{3}y + x - 3 + 2\sqrt{3} = 0$
 (3) $y + \sqrt{3}x + 2 - 3\sqrt{3} = 0$ (4*) $y - \sqrt{3}x + 2 + 3\sqrt{3} = 0$
71. Let $f : (-1, 1) \rightarrow \mathbb{R}$ be a continuous function. If $\int_0^{\sin x} f(t) dt = \frac{\sqrt{3}x}{2}$, then $f\left(\frac{\sqrt{3}}{2}\right)$ is equal to
 (1) $\frac{\sqrt{3}}{2}$ (2) $\sqrt{\frac{3}{2}}$ (3) $\frac{1}{2}$ (4) $\sqrt{3}$
72. Let 10 vertical poles standing at equal distances on a straight line, subtend the same angle of elevation α at a point O on this line and all the poles are on the same side of O . If the height of the longest pole is 'h' and the distance of the foot of the smallest pole from O is 'a'; then the distance between two consecutive poles is
 (1) $\frac{h \cos \alpha - a \sin \alpha}{9 \sin \alpha}$ (2) $\frac{h \sin \alpha + a \cos \alpha}{9 \sin \alpha}$ (3) $\frac{h \sin \alpha + a \cos \alpha}{9 \sin \alpha}$ (4) $\frac{h \cos \alpha - a \sin \alpha}{9 \cos \alpha}$
73. The shortest distance between the z -axis and the line $x + y + 2z - 3 = 0 = 2x + 3y + 4z - 4$, is
 (1) 2 (2) 1 (3) 3 (4) 4
74. If the mean and the variance of a binomial variate X are 2 and 1 respectively, then the probability that X takes a value greater than or equal to one is
 (1) $\frac{1}{16}$ (2) $\frac{3}{4}$ (3) $\frac{15}{16}$ (4) $\frac{9}{16}$
75. The sum of the 3rd and the 4th terms of a G.P. is 60 and the product of its first three terms is 1000. If the first term of this G.P. is positive, then its 7th term is
 (1) 2430 (2*) 320 (3) 640 (4) 7290
76. Let k and K be the minimum and maximum values of the function $f(x) = \frac{(1+x)^{0.6}}{1+x^{0.6}}$ in $[0, 1]$ respectively, then the ordered pair (k, K) is equal to
 (1) $(1, 2^{0.6})$ (2) $(2^{-0.4}, 1)$ (3) $(2^{-0.6}, 1)$ (4) $(2^{-0.4}, 2^{0.6})$

77. If $\cos \alpha + \cos \beta = \frac{3}{2}$ and $\sin \alpha + \sin \beta = \frac{1}{2}$ and θ is the arithmetic mean of α and β , then $\sin 2\theta + \cos 2\theta$ is equal to
- (1) $\frac{8}{5}$ (2) $\frac{4}{5}$ (3) $\frac{3}{5}$ (4*) $\frac{7}{5}$
78. If the lengths of the sides of a triangle are decided by the three throws of a single fair die, then the probability that the triangle is of maximum area given that it is an isosceles triangle, is
- (1) $\frac{1}{27}$ (2) $\frac{1}{26}$ (3) $\frac{1}{21}$ (4) $\frac{1}{15}$
79. If the distance between the foci of an ellipse is half the length of its latus rectum, then the eccentricity of the ellipse is
- (1) $\frac{2\sqrt{2}-1}{2}$ (2) $\frac{1}{2}$ (3) $\sqrt{2}-1$ (4) $\frac{\sqrt{2}-1}{2}$
80. If the incentre of an equilateral triangle is $(1, 1)$ and the equation of its one side is $3x + 4y + 3 = 0$, then the equation of the circumcircle of this triangle is
- (1*) $x^2 + y^2 - 2x - 2y - 14 = 0$ (2) $x^2 + y^2 - 2x - 2y - 7 = 0$
 (3) $x^2 + y^2 - 2x - 2y + 2 = 0$ (4) $x^2 + y^2 - 2x - 2y - 2 = 0$
81. If in a regular polygon the number of diagonals is 54, then the number of sides of this polygon is
- (1) 6 (2) 9 (3) 10 (4*) 12
82. If A is a 3×3 matrix such that $|5 \cdot \text{adj } A| = 5$, then $|A|$ is equal to
- (1) $\pm \frac{1}{5}$ (2) ± 1 (3) ± 5 (4) $\pm \frac{1}{25}$
83. A plane containing the point $(3, 2, 0)$ and the line $\frac{x-1}{1} = \frac{y-2}{5} = \frac{z-3}{4}$ also contains the point
- (1) $(0, 7, 10)$ (2) $(0, 3, 1)$ (3) $(0, 7, -10)$ (4) $(0, -3, 1)$
84. The equation of a normal to the curve $\sin y = x \sin\left(\frac{\pi}{3} + y\right)$ at $x = 0$, is
- (1) $2x - \sqrt{3}y = 0$ (2) $2y + \sqrt{3}x = 0$ (3) $2x + \sqrt{3}y = 0$ (4) $2y - \sqrt{3}x = 0$
85. The solution of the differential equation $ydx - (x + 2y^2)dy = 0$ is $x = f(y)$. If $f(-1) = 1$, then $f(1)$ is equal to
- (1) 3 (2) 2 (3) 1 (4) 4

86. Consider the following statements:

P : Suman is brilliant

Q : Suman is rich

R : Suman is honest

The negation of the statement, "Suman is brilliant and dishonest if and only if Suman is rich" can be equivalently expressed as

- (1) $\sim Q \leftrightarrow \sim P \vee R$ (2) $\sim Q \leftrightarrow P \vee \sim R$ (3) $\sim Q \leftrightarrow P \wedge \sim R$ (4) $\sim Q \leftrightarrow \sim P \wedge R$

87. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a function such that $f(2 - x) = f(2 + x)$ and $f(4 - x) = f(4 + x)$, for all $x \in \mathbb{R}$ and

$\int_0^2 f(x) dx = 5$. Then the value of $\int_{10}^{50} f(x) dx$ is

- (1) 80 (2) 125 (3) 100 (4) 200

88. From the top of a 64 metres high tower, a stone is thrown upwards vertically with the velocity of 48 m/s. The greatest height (in metres) attained by the stone, assuming the value of the gravitational acceleration $g = 32 \text{ m/s}^2$, is

- (1) 112 (2) 88 (3) 128 (4) 100

89. If $\begin{vmatrix} x^2 + x & x + 1 & x - 2 \\ 2x^2 + 3x - 1 & 3x & 3x - 3 \\ x^2 + 2x + 3 & 2x - 1 & 2x - 1 \end{vmatrix} = ax - 12$, then 'a' is equal to

- (1) -24 (2) 24 (3) 12 (4) -12

90. If $\int \frac{\log(t + \sqrt{1+t^2})}{\sqrt{1+t^2}} dt = \frac{1}{2} (g(t))^2 + C$, where C is a constant, then $g(2)$ is equal to

- (1) $\log(2 + \sqrt{5})$ (2) $2\log(2 + \sqrt{5})$ (3) $\frac{1}{2}\log(2 + \sqrt{5})$ (4) $\frac{1}{\sqrt{5}}\log(2 + \sqrt{5})$